



Mini Review on Vector-Like Leptonic Dark Matter, Neutrino Mass, and Collider Signatures

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Specialty section:

This article was submitted to
High-Energy and Astroparticle
Physics,
a section of the journal
Frontiers in Physics

Received: 22 January 2019

Accepted: 06 May 2019

Published: 31 May 2019

Citation:

Bhattacharya S, Ghosh P, Sahoo N
and Sahu N (2019) Mini Review on
Vector-Like Leptonic Dark Matter,
Neutrino Mass, and Collider
Signatures. *Front. Phys.* 7:80.
doi: 10.3389/fphy.2019.00080

We review a class of models in which the Standard Model (SM) is augmented by vector-like leptons: one doublet and a singlet, which are odd under an unbroken discrete Z_2 symmetry. As a result, the neutral component of these additional vector-like leptons are stable and behave as dark matter. We study the phenomenological constraints on the model parameters and elucidate the parameter space for relic density, direct detection and collider signatures of dark matter. In such models, we further add a scalar triplet of hypercharge two and study the consequences. In particular, after electro weak symmetry breaking (EWSB), the triplet scalar gets an induced vacuum expectation value (vev), which yield Majorana masses not only to the light neutrinos but also to vector-like leptonic doublet DM. Due to the Majorana mass of DM, the Z mediated elastic scattering with nucleon is forbidden and hence allowing the model to survive from stringent direct search bound. The DM without scalar triplet lives in a small singlet-doublet leptonic mixing region ($\sin \theta \leq 0.1$) due to large contribution from singlet component and have small mass difference ($\Delta m \sim 10$ GeV) with charged companion, the NLSP (next to lightest stable particle), to aid co-annihilation for yielding correct relic density. Both these observations change to certain extent in presence of scalar triplet to aid observability of hadronically quiet leptonic final states at LHC, while one may also confirm/rule-out the model through displaced vertex signal of NLSP, a characteristic signature of the model in relic density and direct search allowed parameter space.

Keywords: physics beyond the SM, neutrino mass, dark matter, collider signature, dark matter direct detection

1. INTRODUCTION

The existence of dark matter (DM) in a large scale ($>$ a few kpc) has been proven irrefutably by various astrophysical observations. The prime among them are galaxy rotation curves [1, 2], gravitational lensing [3], and large scale structure of the Universe. See for a review [4, 5]. In the recent years the satellite borne experiments like Wilkinson Microwave Anisotropy Probe (WMAP) [6] and PLANCK [7, 8] precisely determined the relic abundance of DM by measuring the temperature fluctuation in the cosmic microwave background radiation (CMBR). All the above said evidences of DM emerge via gravitational interaction in astrophysical environments, which make a challenge to probe the existence of DM in a terrestrial laboratory where density of DM is feeble.

Alternatively one can explore other elementary properties of DM which can be probed at an earth based laboratory. In fact, one can assign a weak interaction property to DM through which it can be thermalized in the early Universe at a temperature above its mass scale. As the temperature falls due to adiabatic expansion of the Universe, the DM gets decoupled from the thermal bath below its mass scale. As a result the ratio: n_{DM}/s , where s is the entropy density, remains constant and is precisely measured by PLANCK in terms of $\Omega_{\text{DM}}h^2 = 0.1186 \pm 0.0020$ [7, 8].

The particle nature of DM, apart from relic abundance, is completely unknown. In particular, the mass, spin, and interaction apart from gravity, etc. This leads to huge uncertainty in search of DM. Despite this, many experiments are currently operational, that uses direct, indirect and collider search methods. Xenon-100 [9], LUX [10], Xenon-1T [11, 12], PANDA [13] are some of the direct DM search experiments which are looking for signature of DM via nuclear scattering, while PAMELA [14, 15], AMS-2 [16], Fermi gamma ray space telescope [17], IceCube [18, 19], etc., are some of the indirect DM search experiments which are looking for signature of DM in the sky. The search of DM is also going on at collider experiments like large Hadron Collider (LHC) [20–22]. Except some excess in the antiparticle flux in the indirect search data, direct and collider searches for DM has produced null observation so far. This in turn put a strong bound on the DM mass and coupling with which it can interact to the visible sector of the universe.

After the Higgs discovery in 2012 at CERN LHC, the standard model (SM) seems to be complete. However, it is found that none of the particles in SM can be a candidate of DM, which is required to be stable on cosmological time scale. While neutrinos in SM are stable, but their relic density is far less than the required DM abundance and is also disfavored from the structure formation. Moreover, neutrinos are massless within the SM. A tiny but non-zero neutrino mass generation requires the SM to be extended. This opens up the possibility of exploring new models of DM, while explaining non-zero masses for neutrinos in the same framework and thus predict a measurable alternation to DM phenomenology, which can be examined in some of the above said experiments.

In this review we explore the possibility of leptonic DM and non-zero neutrino masses [23] in a framework beyond the SM. The simplest leptonic DM can arise by augmenting the SM with an additional singlet fermion [24–42] χ , stabilized by a \mathcal{Z}_2 symmetry. However, unless we assume the presence of an additional scalar singlet, which acquires vacuum expectation value (vev) and thus mixes with SM Higgs, the lepton singlet DM cannot possess renormalizable interaction with visible sector. The next possibility is to introduce a vector-like leptonic doublet: $N = (N^0 \ N^-)^T$, which is also odd under the \mathcal{Z}_2 symmetry. The annihilation cross-section of such fermions are large due to Z mediation and correct relic density can only be achieved at a very high DM mass. However, the combination of singlet χ with the doublet vector-like lepton N provides a good candidate of DM [43–52], which has been discussed in details here. We discuss the phenomenological constraints on model parameters and then elucidate the allowed parameter space of such models from relic density and direct detection constraints. We also indicate collider search strategies for such DM. It turns out that the displaced

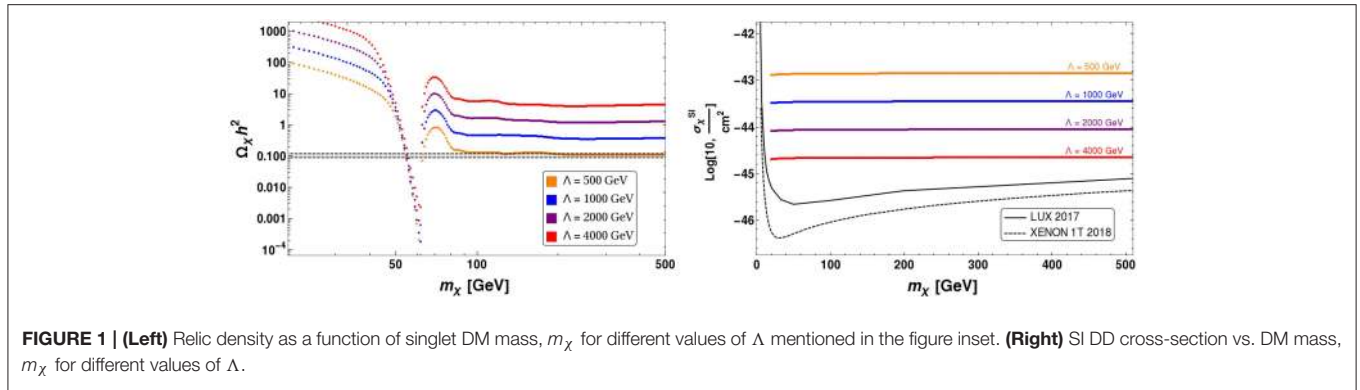
vertex of the charged fermion: N^\pm [also called next to lightest stable particle (NLSP)] is a natural signature of such DM model.

In an attempt to address neutrino mass generation in the same framework, we further add a scalar triplet Δ of hypercharge 2 and study the consequences [53]. In particular, after electro weak symmetry breaking (EWSB), the triplet scalar acquires an induced vacuum expectation value (vev) which give rise sub-eV Majorana masses to light neutrinos through the Type II Seesaw mechanism [54–60]. The scalar triplet also generates a Majorana mass for the neutral component of the vector-like lepton doublet: N^0 , which constitutes a minor component of the DM. Due to Majorana mass of DM, the Z mediated elastic scattering with nucleon is forbidden [61–65]. As a result, the model survives from the stringent direct search bound. In absence of scalar triplet, the singlet-doublet DM is allowed to have only a tiny fraction of doublet component ($\sin\theta \leq 0.1$) to evade direct search bound. In this limit, due to large contribution from the singlet component, the annihilation cross section of the DM becomes smaller than what it requires to achieve correct relic density. To make it up for correct relic density, the DM additionally requires to co-annihilate with its charged and heavy neutral companions and therefore requires small mass difference ($\Delta m \sim 10$ GeV) with charged companion or NLSP. However, in presence of the scalar triplet, we show that both the singlet-doublet mixing ($\sin\theta$) and the mass difference with NLSP (Δm) can be relaxed and larger parameter space is available for correct relic density and being compatible with the latest direct detection bounds. Moreover, the scalar triplet aid observability of hadronically quiet leptonic final states at LHC while one may also confirm/rule-out the model through displaced vertex of NLSP, a characteristic signature of the model in relic density and direct search allowed parameter space.

The paper is arranged as follows. In section 2, we briefly discuss about a vector-like singlet leptonic DM. In section 3, we discuss the viable parameter space of a vector-like inert doublet lepton DM. It is shown that an inert lepton doublet DM alone is ruled out due to large Z -mediated elastic scattering with the nucleus. However, in presence of a scalar triplet of hyper charge-2, the inert lepton doublet DM can be reinstated in a limited parameter space, which we discuss in section 4. Moreover in section 4, we discuss how the scalar triplet can give rise non-zero masses to active neutrinos via type-II seesaw [54–60]. In section 5 we discuss how an appropriate combination of singlet and doublet vector like leptons can give rise a nice possibility of DM in a wide range of parameter space. A triplet extension of singlet-doublet leptonic DM is further discussed in section 6. We discuss collider signature of singlet-doublet leptonic DM in presence of a scalar triplet in section 7 and conclude in section 8. We provide some vertices of inert lepton doublet (ILD) DM in presence of scalar triplet in **Appendix A**.

2. VECTOR-LIKE LEPTONIC SINGLET DARK MATTER

A simplest possibility to explain DM content of the present Universe is to augment the SM by adding a vector-like singlet lepton χ . The stability of χ can be ensured by imposing an



additional discrete Z_2 symmetry, under which χ is odd while all other particles are even. In fact, a singlet DM has been discussed extensively in the literature [24–42]. Here we briefly recapitulate the main features to show the allowed parameter space by observed relic density and latest constraint from direct detection experiments.

The Lagrangian describing the singlet leptonic DM χ can be given as:

$$\mathcal{L} = \bar{\chi} (i\gamma^\mu \partial_\mu - m_\chi) \chi - \frac{1}{\Lambda} (H^\dagger H - \frac{v^2}{2}) \bar{\chi} \chi. \quad (1)$$

Notice that the Lagrangian introduces two new parameters: DM mass, m_χ and the new physics scale Λ connecting DM to the SM through effective dimension five operator, on which the DM phenomenology depends. In the early Universe, χ freezes out via the interaction $\bar{\chi}\chi \rightarrow$ SM particles to give rise a net relic density that we observe today. We use **micrOmegas** [66] to calculate the relic density as well as spin independent elastic cross-section with nucleon of χ . In **Figure 1**, we show relic abundance (left-panel) and spin independent direct detection (SIDD) cross section (right panel) as a function of DM mass (m_χ) for different values $\Lambda \sim \{500 - 4000\}$ GeV¹. We observe that the constraint on SIDD cross section favors large values of Λ , while large Λ values yield over abundance of DM. We also note in the right panel **Figure 1**, that the SIDD cross section is very less sensitive to DM mass. This is because the direct search cross-section is proportional to the effective DM-nucleon reduced mass square ($\mu_r = \frac{m_N m_\chi}{m_N + m_\chi}$) (see Equations 58, 59), where $m_N < m_\chi$ yields a mild dependence on DM mass. This feature is observed in rest of the analysis as well.

Therefore, a singlet leptonic DM alone is almost ruled out. However, the dark sector of the Universe may not be simple as in the case of singlet leptonic DM. In the following we discuss a few more models with larger number of parameters, yet predictive. We end this section by noting that one can think of a pseudoscalar propagator to yield an effective DM-SM interaction of the form $(\bar{\chi}\gamma_5\chi)(H^\dagger H)/\Lambda$. In this case, the relic density and direct search cross-sections become velocity dependent (see for example in Ghorbani [67]). Please also see section 5 below Equation (35) for more details.

¹The scale Λ is a priori unknown and should be validated from experimental constraints. In effective theory consideration, we ensure that $m_\chi < \Lambda$.

3. INERT LEPTON DOUBLET DARK MATTER

Let us assume that the dark sector is composed of a vector-like lepton doublet: $N = (N^0 N^-)^T$, which is odd under an extended Z_2 symmetry [hence called inert lepton doublet (ILD)], while all the Standard Model (SM) fields are even. As a result the neutral component of the ILD N is stable. The quantum numbers of dark sector fields and that of SM Higgs under the SM gauge group, augmented by a Z_2 symmetry, are given in **Table 1**. We will check if N^0 can be a viable candidate of DM with correct relic abundance while satisfying the direct detection constraints from the null observation at various terrestrial laboratories.

The Lagrangian of the model is given as:

$$\mathcal{L}^{IL} = \bar{N} [i\gamma^\mu (\partial_\mu - ig \frac{\sigma^a}{2} W_\mu^a - ig' \frac{Y}{2} B_\mu) - m_N] N. \quad (2)$$

Thus the only new parameter introduced in the above Lagrangian is the mass of N , i.e., m_N . Expanding the covariant derivative of the above Lagrangian \mathcal{L}^{IL} , we get the interaction terms of N^0 and N^\pm with the SM gauge bosons as:

$$\begin{aligned} \mathcal{L}_{int}^{IL} &= \bar{N} i\gamma^\mu (-ig \frac{\sigma^a}{2} W_\mu^a + ig' \frac{Y}{2} B_\mu) N \\ &= \left(\frac{e_0}{2 \sin \theta_W \cos \theta_W} \right) \bar{N}^0 \gamma^\mu Z_\mu N^0 + \frac{e_0}{\sqrt{2} \sin \theta_W} \bar{N}^0 \gamma^\mu W_\mu^+ N^- \\ &\quad + \frac{e_0}{\sqrt{2} \sin \theta_W} N^+ \gamma^\mu W_\mu^- N^0 - e_0 N^+ \gamma^\mu A_\mu N^- \\ &\quad - \left(\frac{e_0}{2 \sin \theta_W \cos \theta_W} \right) \cos 2\theta_W N^+ \gamma^\mu Z_\mu N^-. \end{aligned} \quad (3)$$

where $g = e_0/\sin \theta_W$ and $g' = e_0/\cos \theta_W$ with e_0 being the electromagnetic coupling constant and θ_W being the Weinberg angle.

Since N is a doublet under $SU(2)_L$, it can contribute to invisible Z -decay width if its mass is < 45 GeV which is strongly constrained. Therefore, in our analysis we will assume $m_N > 45$ GeV.

3.1. Relic Abundance of ILD Dark Matter

The number changing annihilation and co-annihilation processes which control freeze-out and hence relic density of DM N^0 are shown in **Figures 2–4**.

To estimate the relic density of DM in this framework one needs to solve the relevant Boltzmann equation:

$$\frac{dn_{N^0}}{dt} + 3Hn_{N^0} = -\langle\sigma v\rangle_{N^0\bar{N}^0\rightarrow SMSM}\left(n_{N^0}^2 - n_{N^0}^{eq\ 2}\right) - \langle\sigma v\rangle_{N^0N^\pm\rightarrow SMSM}\left(n_{N^0}n_{N^\pm} - n_{N^0}^{eq}n_{N^\pm}^{eq}\right). \quad (4)$$

TABLE 1 | Quantum numbers of additional dark sector fermion and SM Higgs under $\mathcal{G} \equiv SU(3)_C \times SU(2)_L \times U(1)_Y \times \mathcal{Z}_2$.

Fields	$SU(3)_C$	\times	$SU(2)_L$	\times	$U(1)_Y$	\times	\mathcal{Z}_2
$N = \begin{pmatrix} N^0 \\ N^- \end{pmatrix}$	1		2		-1		-
$H = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix}$	1		2		1		+

To find the relic density of ILD DM, here we adopted **micrOmegas** [66] and implemented the model in it. Notice that the relic density of DM is mainly controlled by DM mass, m_N and SM gauged couplings. Since SM gauge couplings are fixed, the only relevant parameter which controls the relic density is the DM mass, m_N . The behavior of relic density with DM mass shown in **Figure 5** along with correct relic density bound which is shown in gray patch. Note here that a sharp drop around DM mass $m_N \sim m_h/2$ due to Higgs resonance. From **Figure 5** we can see that the DM mass around $m_N \sim 1$ TeV only satisfy current relic density bound. For heavier mass of N^0 we get over abundance of DM (due to small cross section), while for lighter mass of N^0 we get under abundance of DM (due to large cross-section).

3.2. Direct Search Constraint on ILD Dark Matter

In a direct detection experiment, the DM N^0 scatters with the nucleon through t-channel Z mediated diagram, as shown

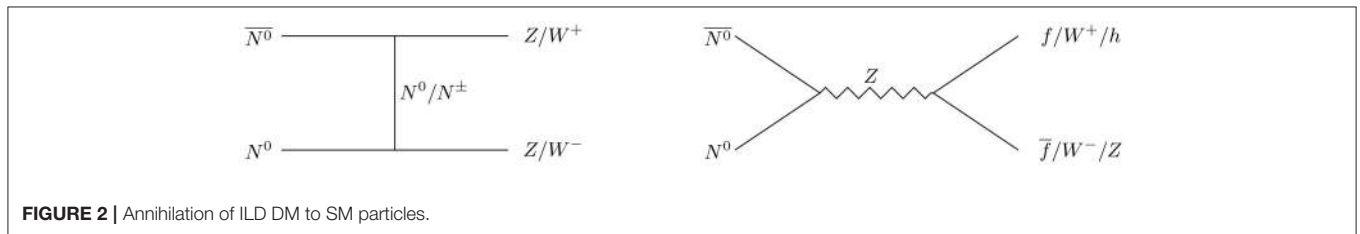


FIGURE 2 | Annihilation of ILD DM to SM particles.

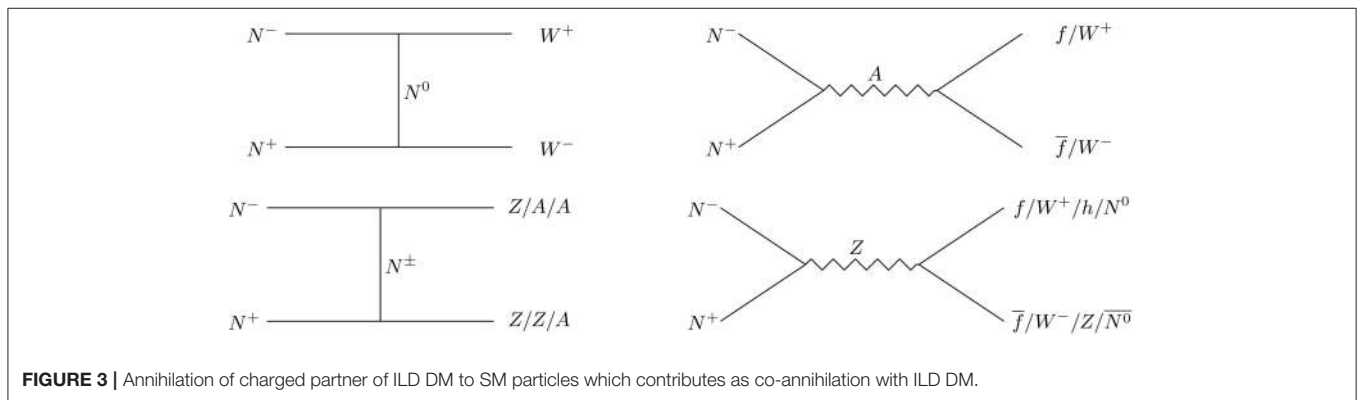


FIGURE 3 | Annihilation of charged partner of ILD DM to SM particles which contributes as co-annihilation with ILD DM.

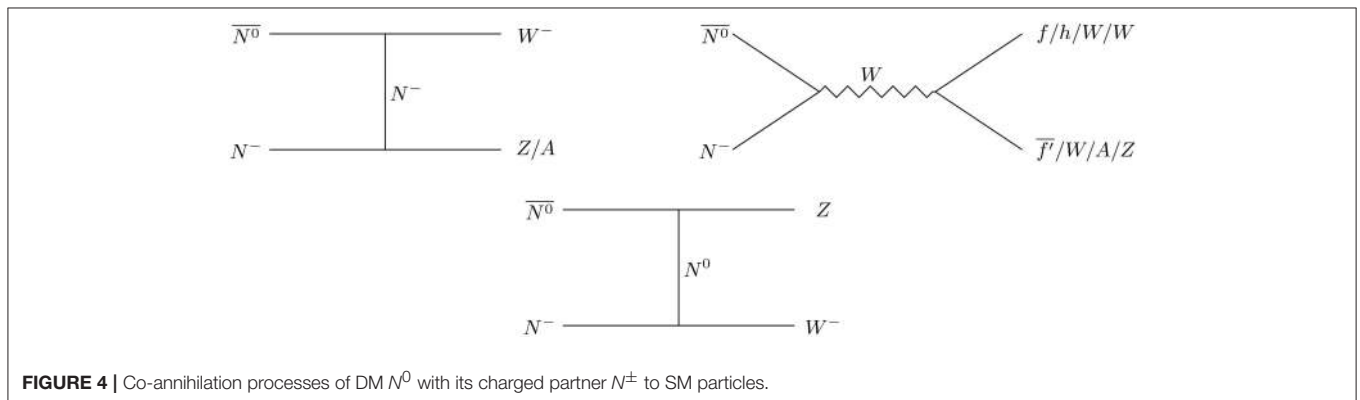
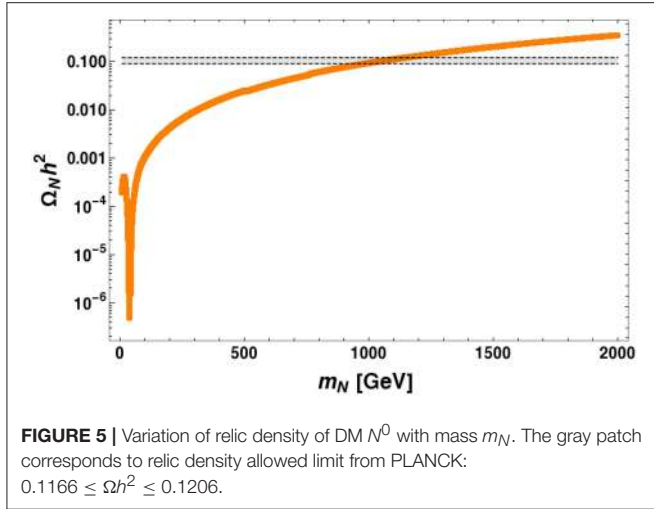


FIGURE 4 | Co-annihilation processes of DM N^0 with its charged partner N^\pm to SM particles.



schematically in the left panel of **Figure 6**. Like relic density we obtain the DM-nucleon cross-section using **micrOmegas** [66]. Since $\bar{N}^0 N^0 Z$ interaction is coming from SM gauge coupling and which is large, so the outcome of spin independent direct detection (SIDD) cross section becomes large. The SIDD cross-section in this case is plotted with DM mass, m_N , which is shown in orange colored patch in right panel of **Figure 6**. The green patch in this **Figure 6** indicates relic density allowed mass range in the same plane. LUX 2017 [10] and XENON 1T [11, 12] direct detection limits are also plotted in the same figure (right panel of **Figure 6**). Thus we see that an ILD DM is completely ruled out by direct detection bound. However, as we discuss in section 4 the ILD DM can be resurrected in presence of a scalar triplet of hyper charge 2. Moreover, the scalar triplet will generate sub-eV masses of active neutrinos through type-II seesaw.

4. TRIPLET EXTENSION OF THE ILD DARK MATTER

We now extend the ILD dark matter model with a scalar triplet, Δ ($Y_\Delta = 2$) which is even under the discrete \mathcal{Z}_2 symmetry. The Lagrangian of this extended sector is given as:

$$\mathcal{L}^{\text{II}} = \text{Tr}[(D_\mu \Delta)^\dagger (D^\mu \Delta)] - V(H, \Delta) + \mathcal{L}_{\text{Yuk}}^{\text{II}}, \quad (5)$$

where the covariant derivative is defined as

$$D_\mu \Delta = \partial_\mu \Delta - ig \left[\frac{\sigma^a}{2} W_\mu^a, \Delta \right] - ig' \frac{Y_\Delta}{2} B_\mu \Delta$$

and in the adjoint representation the triplet Δ can be expressed

$$\text{in a } 2 \times 2 \text{ matrix form: } \Delta = \begin{pmatrix} \frac{H^+}{\sqrt{2}} & H^{++} \\ \delta^0 & -\frac{H^+}{\sqrt{2}} \end{pmatrix}.$$

Similarly the scalar doublet H can be written in component form as:

$$H = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}. \quad (6)$$

The modified scalar potential including Δ and H can be given as:

$$\begin{aligned} V(H, \Delta) = & -\mu_H^2 (H^\dagger H) + \frac{\lambda_H}{4} (H^\dagger H)^2 + M_\Delta^2 \text{Tr}[\Delta^\dagger \Delta] \\ & + \lambda_1 (H^\dagger H) \text{Tr}[\Delta^\dagger \Delta] + \lambda_2 (\text{Tr}[\Delta^\dagger \Delta])^2 \\ & + \lambda_3 \text{Tr}[(\Delta^\dagger \Delta)^2] + \lambda_4 H^\dagger \Delta \Delta^\dagger H \\ & + [\mu (H^T i \sigma^2 \Delta^\dagger H) + \text{h.c.}], \end{aligned} \quad (7)$$

where we assume that M_Δ^2 is positive. So the scalar triplet Δ does not acquire any vev. However, it acquires an induced vev after EW phase transition. The vevs of the scalar fields are given by:

$$\langle \Delta \rangle = \begin{pmatrix} 0 & 0 \\ v_t / \sqrt{2} & 0 \end{pmatrix} \quad \text{and} \quad \langle H \rangle = \begin{pmatrix} 0 \\ v / \sqrt{2} \end{pmatrix}. \quad (8)$$

Since the addition of a scalar triplet can modify the ρ parameter, whose observed value: $\rho = 1.00037 \pm 0.00023$ [68], does not differ much from SM prediction: $\rho = 1$, so we have a constraint on the vev v_t as:

$$v_t \leq 3.64 \text{ GeV}. \quad (9)$$

On the other hand electroweak symmetry breaking gives $\sqrt{v^2 + 2v_t^2} = 246 \text{ GeV}$. This implies that $v_t \ll v$.

Now minimizing the scalar potential, $V(H, \Delta)$ (in Equation 7) we get:

$$\begin{aligned} M_\Delta^2 &= \frac{2\mu v^2 - \sqrt{2}(\lambda_1 + \lambda_4)v^2 v_t - 2\sqrt{2}(\lambda_2 + \lambda_3)v_t^3}{2\sqrt{2}v_t}, \\ \mu_H^2 &= \frac{\lambda_H v^2}{4} + \frac{(\lambda_1 + \lambda_4)v_t^2}{2} - \sqrt{2}\mu v_t. \end{aligned} \quad (10)$$

In the limit $v_t \ll v$, from Equation (10) we get the vevs,

$$v_t = \frac{\mu v^2}{M_\Delta^2 + (\lambda_1 + \lambda_4)v^2/2} \quad \text{and} \quad v \approx \frac{2\mu_H}{\sqrt{\lambda_H}}. \quad (11)$$

In presence of the scalar triplet Δ , the Yukawa interactions in Equation (5) are given by:

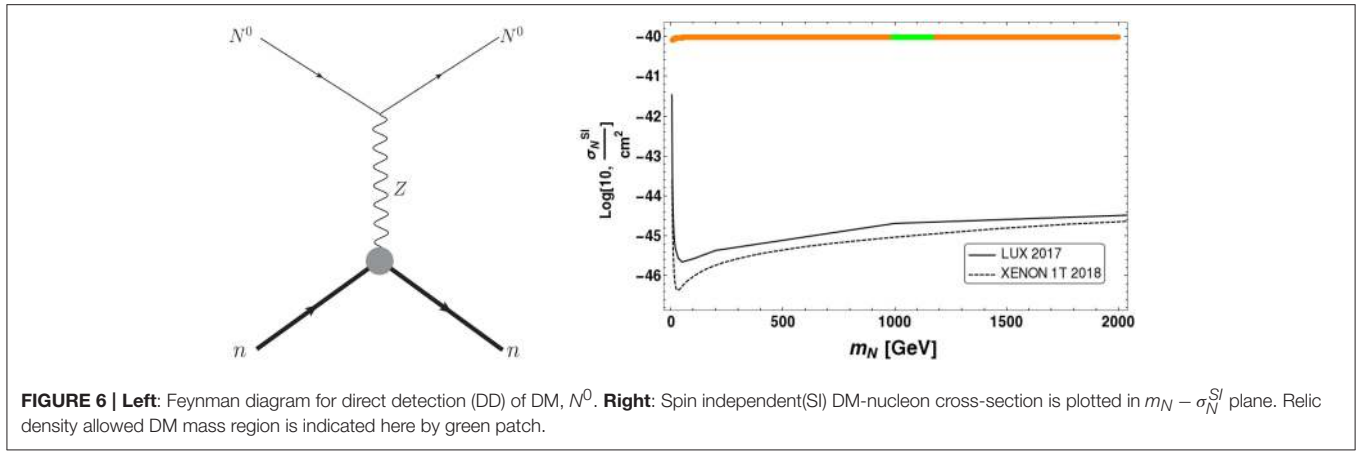
$$\mathcal{L}_{\text{Yuk}}^{\text{II}} = \frac{1}{\sqrt{2}} [(f_L)_{\alpha\beta} \bar{L}_\alpha^c i \sigma^2 \Delta L_\beta + f_N \bar{N}^c i \sigma^2 \Delta N + \text{h.c.}], \quad (12)$$

where L is the SM lepton doublet and α, β denote family indices. The Yukawa interactions importantly inherit the source of neutrino masses (first term in square bracket) and DM-SM interactions (second term in square bracket).

4.1. Scalar Doublet-Triplet Mixing

The quantum fluctuations around the minimum of scalar potential, $V(H, \Delta)$ can be given as:

$$\Delta = \begin{pmatrix} \frac{H^+}{\sqrt{2}} & H^{++} \\ \frac{v_t + h_t + iA^0}{\sqrt{2}} & -\frac{H^+}{\sqrt{2}} \end{pmatrix} \quad \text{and} \quad H = \begin{pmatrix} 0 \\ \frac{v+h}{\sqrt{2}} \end{pmatrix}. \quad (13)$$



Thus the scalar sector constitute two CP-even Higgses: h and h_t , one CP-odd Higgs: A^0 , one singly charged scalar: H^{\pm} and one doubly charged scalar: $H^{\pm\pm}$. In the limit $v_t \ll v$, the mass matrix of the CP-even Higgses: h and h_t , is given by:

$$\mathcal{M}^2 = \begin{pmatrix} m_h^2 & -\sqrt{2}\mu v \\ -\sqrt{2}\mu v & m_T^2 \end{pmatrix}, \quad (14)$$

where $m_h^2 \approx \lambda_H v^2/2$ and $m_T^2 = \mu v^2/\sqrt{2}v_t$. Diagonalizing the above mass matrix we get two neutral physical Higgses: H_1 and H_2 :

$$H_1 = \cos \alpha h + \sin \alpha h_t, \quad H_2 = -\sin \alpha h + \cos \alpha h_t, \quad (15)$$

where H_1 is the standard model like Higgs and H_2 is the triplet like scalar. The corresponding mass eigenvalues are m_{H_1} (SM like Higgs) and m_{H_2} (triplet like scalar) are given by:

$$\begin{aligned} m_{H_1}^2 &\approx m_h^2 - \frac{(\mu v/\sqrt{2})^2}{m_T^2 - m_h^2}, \\ m_{H_2}^2 &\approx m_T^2 + \frac{(\mu v/\sqrt{2})^2}{m_T^2 - m_h^2}. \end{aligned} \quad (16)$$

The mixing angle is given by

$$\tan 2\alpha = \frac{-\sqrt{2}\mu v}{(m_T^2 - m_h^2)}. \quad (17)$$

From Equations (9, 11, 17) we see that there exist an upper bound on the mixing angle

$$\sin \alpha < 0.02 \left(\frac{174 \text{ GeV}}{v} \right) \left(\frac{1}{1 - 0.39 \frac{(m_h/125 \text{ GeV})^2}{(m_T/200 \text{ GeV})^2}} \right). \quad (18)$$

We also get a constraint on $\sin \alpha$ from SM Higgs phenomenology, since the mixing can change the strength of the Higgs coupling to different SM particles. See for example [69, 70], in which

the global fit yields a constraint on mixing angle $\sin \alpha \lesssim 0.5$, which is much larger than the above constraint obtained using ρ parameter.

From Equation (7), all the couplings $\lambda_H, \lambda_1, \lambda_2, \lambda_3, \lambda_4$ and μ can be expressed in terms of physical scalar masses: $m_{H_1}, m_{H_2}, m_{H^{\pm}}, m_{H^{\pm\pm}}, m_{A^0}$ and the vevs v and v_t as Arhrib et al. [71]:

$$\begin{aligned} \lambda_H &= \frac{2}{v^2} (m_{H_1}^2 \cos^2 \alpha + m_{H_2}^2 \sin^2 \alpha), \\ \lambda_1 &= \frac{4m_{H^{\pm}}^2}{v^2 + 4v_t^2} - \frac{2m_{A^0}^2}{v^2 + 4v_t^2} + \frac{\sin 2\alpha}{2v_t v} (m_{H_1}^2 - m_{H_2}^2), \\ \lambda_2 &= \frac{1}{v_t^2} \left[\frac{1}{2} (m_{H_1}^2 \sin^2 \alpha + m_{H_2}^2 \cos^2 \alpha) + \frac{v^2}{2(v^2 + 4v_t^2)} m_{A^0}^2 \right. \\ &\quad \left. - \frac{2v^2}{v^2 + 4v_t^2} m_{H^{\pm}}^2 + m_{H^{\pm\pm}}^2 \right], \\ \lambda_3 &= \frac{1}{v_t^2} \left[\frac{2v^2}{v^2 + 2v_t^2} m_{H^{\pm}}^2 - \frac{v^2}{v^2 + 4v_t^2} m_{A^0}^2 - m_{H^{\pm\pm}}^2 \right], \\ \lambda_4 &= \frac{4m_{A^0}^2}{v^2 + 4v_t^2} - \frac{4m_{H^{\pm}}^2}{v^2 + 2v_t^2}, \\ \mu &= \frac{\sqrt{2}v_t}{v^2 + 4v_t^2} m_{A^0}^2. \end{aligned} \quad (19)$$

where m_{A^0} is the mass of pseudo scalar. It is important to note that the quartic couplings λ_2 and λ_3 are inversely proportional to the triplet vev v_t which has important consequences for dark matter relic abundance that we discuss in section 4.4.

4.2. Non-zero Neutrino Masses

The coupling of scalar triplet Δ to SM lepton and Higgs doublet combinely break the lepton number by two units as given in Equation (12). As a result the $\Delta L_\alpha L_\beta$ coupling yields Majorana masses to three flavors of active neutrinos as Magg and Wetterich [54], Lazarides et al. [55], Mohapatra and Senjanovic [56], Ma and Sarkar [57], Konetschny and Kummer [58], Schechter and Valle [59], Cheng and Li [60]:

$$(M_\nu)_{\alpha\beta} = \sqrt{2}(f_L)_{\alpha\beta} \langle \Delta \rangle \approx (f_L)_{\alpha\beta} \frac{-\mu v^2}{\sqrt{2}M_\Delta^2}. \quad (20)$$

Assuming $\mu \simeq M_\Delta \simeq \mathcal{O}(10^{13})$ GeV, we can explain neutrino masses of order 1eV with a coupling strength $f_L \simeq 1$. However, the scale of M_Δ can be brought down to \sim TeV by taking the coupling to be much smaller $f_L \simeq 10^{-11}$, and indeed represents a bit of fine tuning in the neutrino sector.

To get the neutrino mass eigen values, the above mass matrix can be diagonalized by the usual U_{PMNS} matrix as :

$$M_\nu = U_{PMNS} M_\nu^{diag} U_{PMNS}^T, \tag{21}$$

where U_{PMNS} is given by

$$U_{PMNS} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{13}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{13}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{13}} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta_{13}} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta_{13}} & c_{23}c_{13} \end{pmatrix} \cdot U_{ph}, \tag{22}$$

with c_{ij} , s_{ij} stand for $\cos\theta_{ij}$ and $\sin\theta_{ij}$ respectively and U_{ph} is given by

$$U_{ph} = \text{Diag}(e^{-i\gamma_1}, e^{-i\gamma_2}, 1). \tag{23}$$

Where γ_1, γ_2 are two Majorana phases. The diagonal matrix $M_\nu^{diag} = \text{Diag}(m_1, m_2, m_3)$ with diagonal entries are the mass eigen values for the neutrinos. The current neutrino oscillation data at 3σ confidence level give the constraint on mixing angles [68] :

$$0.259 < \sin^2\theta_{12} < 0.359, 0.374 < \sin^2\theta_{23} < 0.628, 0.0176 < \sin^2\theta_{13} < 0.0295. \tag{24}$$

However little information is available about the CP violating Dirac phase δ as well as the Majorana phases. Although the absolute mass of neutrinos is not measured yet, the mass square differences have already been measured to a good degree of accuracy :

$$\Delta m_0^2 \equiv m_2^2 - m_1^2 = (6.99 - 8.18) \times 10^{-5} \text{eV}^2$$

$$|\Delta m_{\text{atm}}^2| \equiv |m_3^2 - m_1^2| = (2.23 - 2.61) \times 10^{-3} \text{eV}^2. \tag{25}$$

One of the main issues of neutrino physics lies in the sign of the atmospheric mass square difference $|\Delta m_{\text{atm}}^2| \equiv |m_3^2 - m_1^2|$, which is still unknown. This yields two possibilities: normal hierarchy (NH) ($m_1 < m_2 < m_3$) or inverted hierarchy (IH) ($m_3 < m_1 < m_2$). Another possibility, yet allowed, is to have a degenerate (DG) neutrino mass spectrum ($m_1 \sim m_2 \sim m_3$). Assuming that the neutrinos are Majorana, the mass matrix can be written as:

$$M_\nu = \begin{pmatrix} a & b & c \\ b & d & e \\ c & e & f \end{pmatrix}. \tag{26}$$

Using equations (21), (22), (24) and (25), we can estimate the unknown parameters in neutrino mass matrix of Equation (26). To estimate the parameters in NH, we use the best fit values of the oscillation parameters. For a typical value of the lightest neutrino mass of $m_1 = 0.0001$ eV, we get the mass parameters (in eV) as :

$$a = 0.003833, b = 0.00759, c = 0.002691,$$

$$d = 0.023865, e = 0.02083, f = 0.03038. \tag{27}$$

Similarly for IH case, choosing the lightest neutrino mass $m_3 = 0.001$ eV, we get the mass parameters (in eV) as :

$$a = 0.0484, b = -0.00459, c = -0.00573,$$

$$d = 0.02893, e = -0.02366, f = 0.02303. \tag{28}$$

In both the cases, we put the Dirac and Majorana phases to be zero for simplicity.

The analysis of neutrino mass is more indicative here than being exhaustive. This is essentially to build the connection between the dark sector and neutrino sector advocated in the model set up. One can easily perform a scan over the mass matrix parameters to obtain correct ranges of the neutrino observables, and that of course lies in the vicinity of the aforementioned values. But, we do not aim to elaborate that in this draft. We have not also adhered to a specific lepton mixing matrix pattern (say tri-bi-maximal mixing) coming from a defined underlying flavor symmetry (say A_4), which will be able to correlate different parameters of the mass matrix.

The mass of the scalar triplet can also be brought down to TeV scale by choosing appropriate Yukawa coupling as explained before. If the triplet mass is order of a few hundreds of GeV, then it can give interesting dilepton signals in the collider. See for example, [72–78] for a detailed discussion regarding the dilepton signatures of the scalar triplet at collider.

4.3. Pseudo-Dirac Nature of ILD Dark Matter

From Equation (12) we see that the vev of Δ induces a Majorana mass to N^0 which is given by:

$$m = \sqrt{2}f_N \langle \Delta \rangle \approx f_N \frac{-\mu v^2}{\sqrt{2}M_\Delta^2}. \tag{29}$$

Thus the N^0 has a large Dirac mass M_N (as in Equation 2) and a small Majorana mass m as shown in the above Equation (29). Therefore, we get a mass matrix in the basis $\{N_L^0, (N_R^0)^c\}$ as:

$$\mathcal{M} = \begin{pmatrix} m & M_N \\ M_N & m \end{pmatrix}. \tag{30}$$

Thus the Majorana mass m splits the Dirac spinor N^0 into two pseudo-Dirac states $N_{1,2}^0$ with mass eigenvalues $M_N \pm m$. The mass splitting between the two pseudo-Dirac states $N_{1,2}^0$ is given by

$$\delta m = 2m = 2\sqrt{2}f_N \langle \Delta \rangle. \tag{31}$$

Note that $\delta m \ll M_N$ from the estimate of induced vev of the triplet and hence does not play any role in the relic abundance calculation. However, the sub-GeV order mass splitting plays a crucial role in direct detection by forbidding the Z-boson mediated DM-nucleon elastic scattering. Now from Equations (20, 29) we see that the ratio:

$$R = \frac{(M_\nu)}{m} = \frac{f_L}{f_N} \lesssim 10^{-5}, \tag{32}$$

where we assume $M_\nu \sim 1$ eV and $m \sim 100$ keV. Here the mass splitting between the two states N_1^0 and N_2^0 is chosen to be $\mathcal{O}(100)$ keV in order to forbid the Z -mediated inelastic scattering with the nucleons in direct detection. Thus, we see that the ratio $R \lesssim 10^{-5}$ is heavily fine tuned. In other words, the scalar triplet strongly decay to ILD dark matter, while its decay to SM leptons is suppressed.

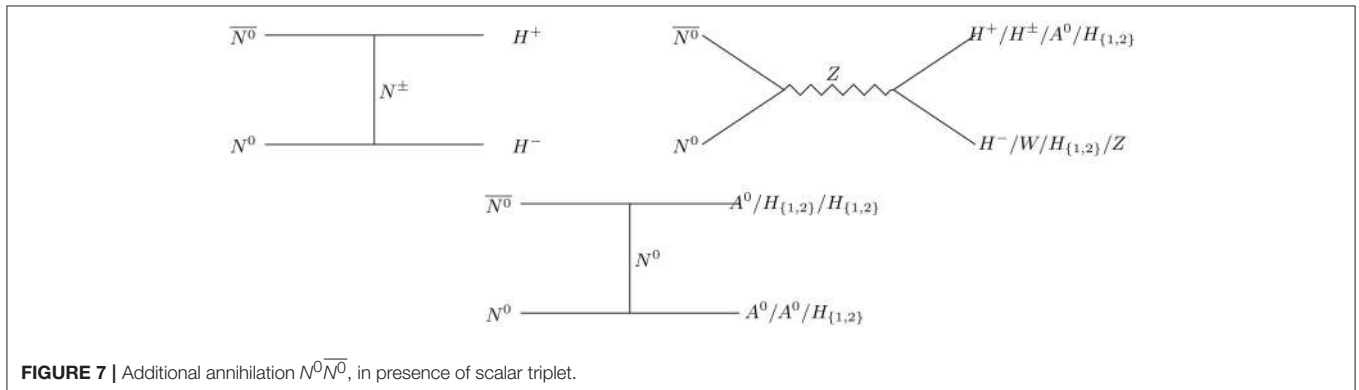
4.4. Effect of Scalar Triplet on Relic Abundance of ILD Dark Matter

In presence of a scalar triplet, when the DM mass is larger than the triplet mass, a few additional annihilation and co-annihilation channels open up as shown in **Figures 7–10** in addition to the previously mentioned Feynman diagrams given in **Figures 2–4**. These additional channels also play a key role in number changing processes of DM, N^0 to yield a modified freeze-out abundance. We numerically calculate relic density of N^0 DM once again by implementing the model in the code **micrOmegas** [66]. The parameter space, in comparison to the ILD dark matter alone, is enhanced due to the additional coupling of N^0 with Δ . In particular, the new parameters are: triplet scalar masses $m_{H_2}, m_{A^0}, m_{H^\pm}, m_{H^{\pm\pm}}$, vev of scalar triplet v_t , coupling of scalar triplet with ILD dark matter N^0 , i.e., f_N , scalar doublet-triplet mixing $\sin \alpha$.

To understand the effect of the triplet scalar on relic density of ILD DM, we show in **Figure 11** the variation of relic density as a function of DM mass (m_N) with different choices of triplet vev (v_t) while keeping a fixed f_N and $\sin \alpha$. In the left panel of **Figure 11** we choose the scalar doublet-triplet mixing to be $\sin \alpha = 0.001$ while in the right-panel of **Figure 11** we choose $\sin \alpha = 0.1$. In both cases we set the physical CP even, CP odd and charged triplet scalar masses respectively at $m_{H_2} = 280, m_{A^0} = 280, m_{H^\pm} = 300$ and $m_{H^{\pm\pm}} = 310$ GeV and $f_N = 0.1$. We note that there is a resonance drop near $m_N \sim m_Z/2$ as usual for Z mediated s -channel diagrams. Additionally we find that near $m_N \sim 280$ GeV (which is the mass of H_2), relic density drops suddenly because of new annihilation processes $NN \rightarrow \Delta\Delta$ start to contribute (see diagrams in **Figures 7–10**). With larger triplet vev $v_t \sim \text{GeV}$, the effect of annihilation to scalar triplet becomes subdued. This can be understood as follows. First of all, we see that the

quartic couplings involving the triplet, as given in Equation (19), are inversely proportional to the triplet vev (v_t). In a typical annihilation process: $N^- \bar{N}^{-c} \rightarrow H^- H^-$, mediated by H^{--} , the vertex $H^{--} H^- H^-$ is proportional to $\sqrt{2} v_t \lambda_3 \sim 1/v_t$, which diminishes with larger v_t . On the other hand, let us consider the process: $N^0 \bar{N}^{0c} \rightarrow H^{++} H^{--}$, which has a significant contribution to the total relic density. This process is mediated by H_1 and H_2 . In small $\sin \alpha$ limit, the H_1 mediated diagram is vanishingly small as the $N^0 \bar{N}^0 H_1 \sim \sin \alpha$. So, H_2 mediation dominates here. However, the vertex involving $H_2 H^{++} H^{--}$ is proportional to $(2 \cos \alpha \lambda_2 v_t - \sin \alpha \lambda_1 v_d)$. One can see that for small v_t , the first term is negligible, while for a larger v_t , the first term becomes comparable to that of the second one and has a cancelation. This cancelation therefore decreases the annihilation cross-section to the chosen final state. Such a phenomena is also present for co-annihilation processes like $N^- \bar{N}^{-c} \rightarrow H^- H_2$ etc., where the vertices involve a combination of λ_1 , and λ_2 . On the other hand, for smaller values of triplet vev ($v_t \sim 0.01$ GeV), there is a larger drop in relic density due to the additional annihilation channels (to the triplet scalars as mentioned). Therefore, the DM N^0 achieves correct relic density for larger DM mass m_N (as compared to that of the case in absence of triplet). Moreover, we set $f_N = 0.1$ in both cases. It is straightforward to see that annihilation to the triplet final states are proportional to f_N . Therefore, with larger f_N , the drop in relic density in the vicinity of triplet scalar mass decreases even further. In summary, the presence of scalar triplet shifts the relic density of ILD DM to a higher DM mass region which crucially depends on the choice of the triplet vev as well as ΔNN coupling f_N .

An important conclusion about ILD dark matter is that the mass of DM (m_N) is around 1 TeV which satisfies the observed relic abundance. This implies the mass of N^- , the charged partner of N^0 , is about 1 TeV as well. However, the electroweak correction induces a small mass splitting between N^0 and N^- to be around 162 MeV. Therefore, N^- can give rise a displaced vertex signature through the 3-body decay $N^- \rightarrow N^0 \ell^- \bar{\nu}_\ell$ [79]. But the main drawback is that the production cross-section of N^\pm of mass $\sim \text{TeV}$ is highly suppressed at LHC as this can only be possible through Drell-Yan. Therefore, in section 5 we discuss a more predictive model by enlarging the dark sector with an additional singlet fermion χ .



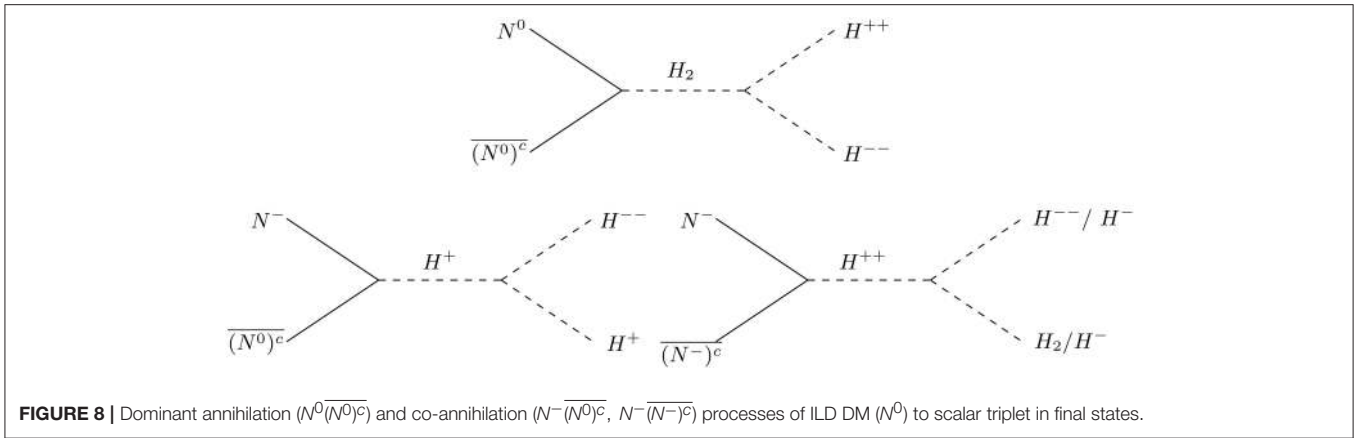


FIGURE 8 | Dominant annihilation ($N^0\overline{(N^0)^c}$) and co-annihilation ($N^-\overline{(N^0)^c}$, $N^-\overline{(N^-)^c}$) processes of ILD DM (N^0) to scalar triplet in final states.

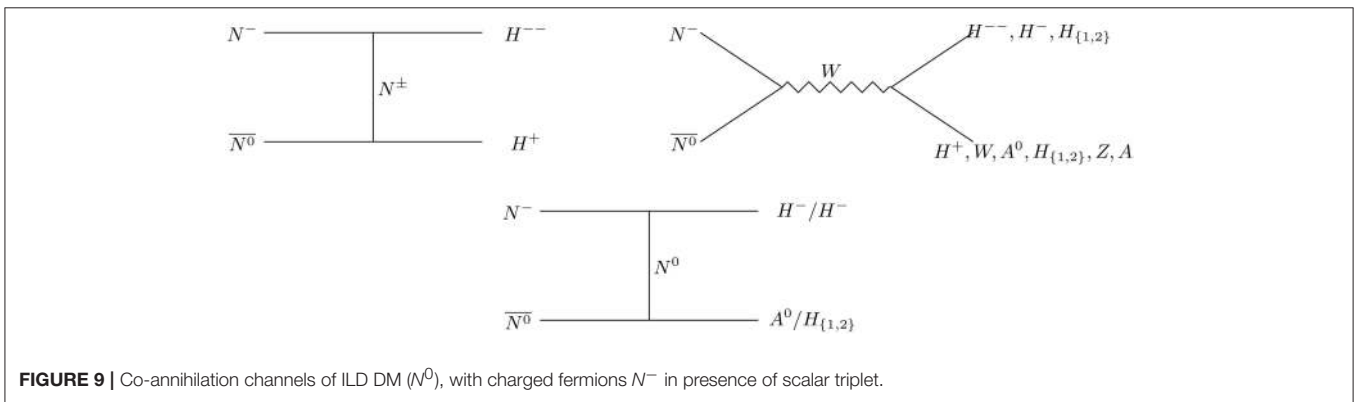


FIGURE 9 | Co-annihilation channels of ILD DM (N^0), with charged fermions N^- in presence of scalar triplet.

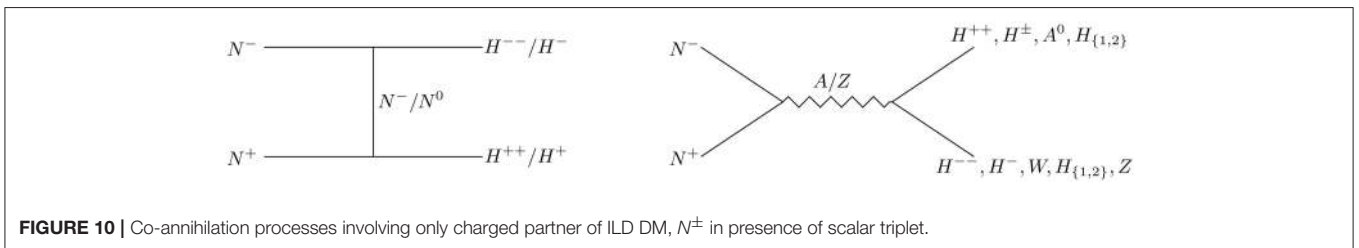


FIGURE 10 | Co-annihilation processes involving only charged partner of ILD DM, N^\pm in presence of scalar triplet.

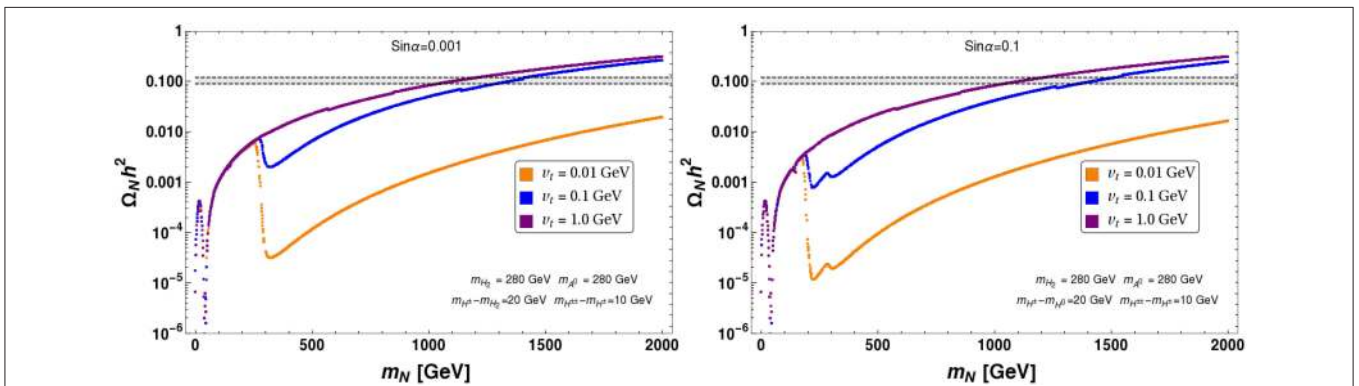


FIGURE 11 | Relic density vs. m_N plot for different choices triplet vev, v_t , keeping $\sin\alpha = 0.001$ (left) and $\sin\alpha = 0.1$ (right). Others parameters are mentioned in the figure. The gray patch indicates relic density bounds. In both cases we set $f_N = 0.1$.

4.5. Effect of Salar Triplet on Direct Detection of ILD Dark Matter

As discussed in section 3.2, the ILD dark matter alone is ruled out due to large Z-mediated elastic scattering with nucleus. However, it can be reinstated in presence of the scalar triplet, which not only forbids the Z-mediated elastic scattering [61–65] but also provides a new portal for the detection of ILD dark matter via the doublet-triplet mixing as we discuss below.

The interaction of DM with the Z boson with the kinetic term is given as

$$\mathcal{L}_{Z-DM} \supset i\bar{N}^0 (\gamma^\mu \partial_\mu - ig_Z \gamma^\mu Z_\mu) N^0, \quad (33)$$

where $ig_Z = \frac{g}{2\cos\theta_W}$. After the symmetry breaking the scalar triplet Δ gets an induced vev and hence gives Majorana mass to the ILD dark matter N_0 as shown in Equation (29). The presence of such Majorana mass term splits the Dirac DM state into two real Majorana states N_1^0 and N_2^0 with a mass splitting of δm as discussed in section 4.3. Now we rewrite the Lagrangian involving DM-Z interaction in terms of the new Majorana states as:

$$\mathcal{L}_{Z-DM} \supset \bar{N}_1^0 i\gamma^\mu \partial_\mu N_1^0 + \bar{N}_2^0 i\gamma^\mu \partial_\mu N_2^0 - ig_Z \bar{N}_1^0 \gamma^\mu N_2^0 Z_\mu. \quad (34)$$

We can see that the dominant gauge interaction becomes off-diagonal. The absence of diagonal interaction term for the DM-Z vertex leads to the vanishing contribution to elastic scattering of the DM with the nucleus. However, there could be an inelastic scattering through Z mediation, which is suppressed if the mass splitting between two states is of the order $\mathcal{O}(100)$ keV or less. But the Yukawa term involving DM and Δ is still diagonal in the new basis and hence can lead to elastic scattering through a mixing between the doublet-triplet Higgs. Assuming N_1^0 to be the lightest among the two Majorana states, hence being the DM, the relevant diagram for the elastic scattering is shown in **Figure 12**.

The direct detection cross-section mainly depends on m_{H_2}, f_N and $\sin\alpha$. We have plotted the spin independent direct detection cross-section as a function of the DM mass $m_{N_1^0}$ in **Figure 13**. Keeping $m_{H_2} = 280$ GeV (Solid) and $m_{H_2} = 600$ GeV (Dashed) fixed, we have shown the cross-section for three different values $\{f_N = 0.01, 0.1, 1\}$ in Red, Blue, and Green color, respectively. Since there is a relative negative sign between the two amplitudes, the destructive interference is more for m_{H_2} comparable to SM Higgs. Hence cross section for $m_{H_2} = 280$ GeV turns out to be smaller than $m_{H_2} = 600$ GeV. But if we increase the mass of m_{H_2} to TeV scale then H_2 mediated process will be suppressed due to the large mass in the propagator and only H_1 mediated process will contribute. The direct search cross-section increases with larger Yukawa coupling f_N from 0.01 to 1 and can be easily seen from the **Figure 13**. Since the DM couples dominantly to the triplet scalar, the more the mixing angle ($\sin\alpha$), the more is the cross-section which can be clearly seen from the left and right panel of **Figure 13**. But all these cross-sections are well below the present experimental bound of LUX and Xenon-1T. Note that the relic density allowed parameter space of ILD DM in presence of a scalar triplet live in a very high DM mass region $\sim TeV$ with moderate f_N and Higgs data unambiguously indicates that the

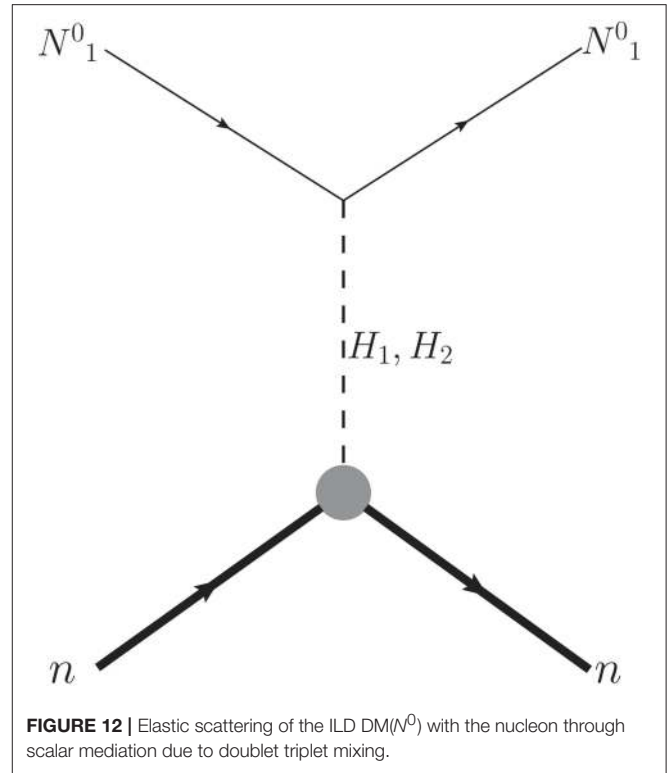


FIGURE 12 | Elastic scattering of the ILD DM(N^0) with the nucleon through scalar mediation due to doublet triplet mixing.

mixing angle ($\sin\alpha$) should be kept small, as we have shown in **Figure 13**. Therefore, the ILD becomes a viable DM candidate in the presence of a triplet scalar allowed by both relic density and direct search constraints.

5. SINGLET-DOUBLET LEPTONIC DARK MATTER

Now let us assume that the dark sector is composed of two vector like leptons : a doublet, $N = (N^0 N^-)^T$ and a singlet χ , which are odd under an extended \mathcal{Z}_2 symmetry while all the Standard Model (SM) fields are even. As a result the lightest odd particle in the dark sector is stable and behave as a candidate of DM. The quantum numbers of dark sector fields and that of SM Higgs under the SM gauge group, augmented by a \mathcal{Z}_2 symmetry, are given in **Table 2**.

The Lagrangian of the model can be given as follows:

$$\mathcal{L}^{VF} = \bar{N} [i\gamma^\mu (\partial_\mu - ig \frac{\sigma^a}{2} W_\mu^a - ig' \frac{Y}{2} B_\mu) - m_N] N + \bar{\chi} (i\gamma^\mu \partial_\mu - m_\chi) \chi - (Y_1 \bar{N} \tilde{H} \chi + h.c). \quad (35)$$

Note that here we have assumed to have a CP conserving interaction between the additional vector like fermion to the SM Higgs. One may also think of a coupling $-(Y_1 \bar{N} \gamma_5 \tilde{H} \chi + h.c)$ that will violate CP. Now, it is a bit intriguing to think of such interactions before the debate on the SM Higgs to be a scalar or a pseudoscalar is settled. The outcome of such an interaction will alter the subsequent phenomenology significantly. For example, it is known that advocating a pseudoscalar (S) interaction to a vector like DM (ψ), for example,

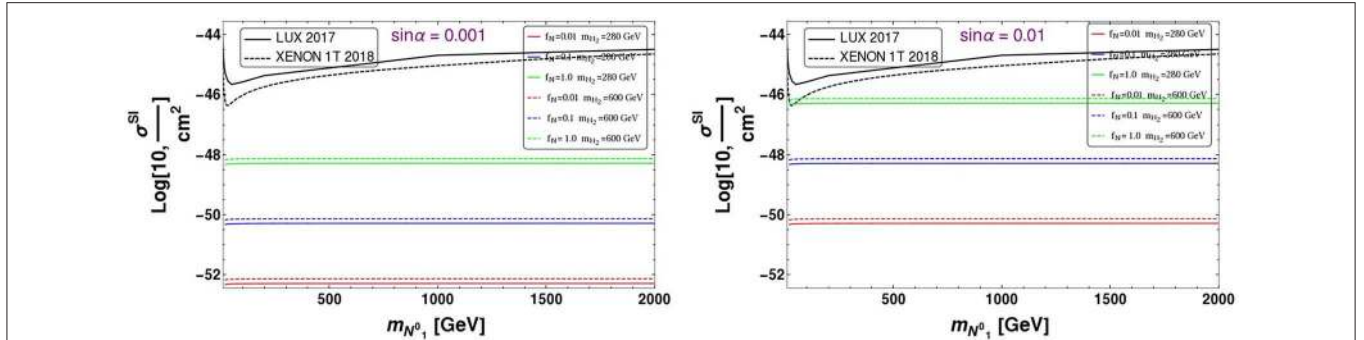


FIGURE 13 | SI direct detection cross-section σ^{SI} as a function of DM mass m_{N^0} for $\sin \alpha = 0.001$ (Left) and $\sin \alpha = 0.01$ (Right). Different choices of the coupling $\{f_N = 0.01, 0.1, 1\}$ are shown in Red, Blue, and Green color, respectively. Dashed and solid lines corresponds to different values of the heavy Higgs $m_{H_2} = 600, 280$ GeVs, respectively. The bound from LUX 2017 and XENON1T 2018 are shown.

TABLE 2 | Quantum numbers of additional dark sector fermions and that of Higgs under $\mathcal{G} \equiv SU(3)_C \times SU(2)_L \times U(1)_Y \times \mathcal{Z}_2$.

Fields	$SU(3)_C$	\times	$SU(2)_L$	\times	$U(1)_Y$	\times	\mathcal{Z}_2
$N = \begin{pmatrix} N^0 \\ N^- \end{pmatrix}$	1		2		-1		-
χ	1		1		0		-
$H = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix}$	1		2		1		+

with a term like $-yS\bar{\psi}\gamma_5\psi$ indicates that DM-nucleon scattering becomes velocity dependent and therefore reduces the direct search constraint significantly to allow the model live in a larger allowed parameter space. However, the Yukawa interaction term itself ($-yS\bar{\psi}\gamma_5\psi$) do not violate parity as S is assumed to be pseudoscalar by itself (see for example in Ghorbani [67]).

After Electroweak symmetry breaking (EWSB) the SM Higgs acquires a vacuum expectation value v . The quantum field around the vacuum can be given as: $H = \begin{pmatrix} 0 \\ \frac{1}{\sqrt{2}}(v+h) \end{pmatrix}^T$ where $v = 246$ GeV. The presence of the Yukawa term: $Y_1\bar{N}\tilde{H}\chi$ term in the Lagrangian (Equation 35), arises an admixture between N^0 and χ . The bare mass terms of the vector like fermions in \mathcal{L}^{VF} then take the following form:

$$\begin{aligned}
 -\mathcal{L}_{mass}^{VF} &= m_N\bar{N}^0N^0 + m_N N^+N^- + m_\chi\bar{\chi}\chi + \frac{Y_1v}{\sqrt{2}}\bar{N}^0\chi \\
 &\quad + \frac{Y_1v}{\sqrt{2}}\bar{\chi}N^0 \\
 &= \overline{(\chi \ N^0)} \begin{pmatrix} m_\chi & \frac{Y_1v}{\sqrt{2}} \\ \frac{Y_1v}{\sqrt{2}} & m_N \end{pmatrix} \begin{pmatrix} \chi \\ N^0 \end{pmatrix} + m_N N^+N^-. \quad (36)
 \end{aligned}$$

The unphysical basis, $(\chi \ N^0)^T$ is related to physical basis, $(N_1 \ N_2)^T$ through the following unitary transformation:

$$\begin{pmatrix} \chi \\ N^0 \end{pmatrix} = \mathcal{U} \begin{pmatrix} N_1 \\ N_2 \end{pmatrix} = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} N_1 \\ N_2 \end{pmatrix}, \quad (37)$$

where the mixing angle

$$\tan 2\theta = -\frac{\sqrt{2}Y_1v}{m_N - m_\chi}. \quad (38)$$

The mass eigenvalues of the physical states N_1 and N_2 are respectively given by:

$$\begin{aligned}
 m_{N_1} &= m_\chi \cos^2\theta + m_N \sin^2\theta + \frac{Y_1v}{\sqrt{2}} \sin 2\theta \\
 m_{N_2} &= m_\chi \sin^2\theta + m_N \cos^2\theta - \frac{Y_1v}{\sqrt{2}} \sin 2\theta \quad (39)
 \end{aligned}$$

For small $\sin\theta$ ($\sin\theta \rightarrow 0$) limit, m_{N_1} and m_{N_2} can be further expressed as:

$$\begin{aligned}
 m_{N_1} &\simeq m_\chi + \frac{Y_1v}{\sqrt{2}} \sin 2\theta \equiv m_\chi - \frac{(Y_1v)^2}{(m_N - m_\chi)}, \\
 m_{N_2} &\simeq m_N - \frac{Y_1v}{\sqrt{2}} \sin 2\theta \equiv m_N + \frac{(Y_1v)^2}{(m_N - m_\chi)}. \quad (40)
 \end{aligned}$$

Here we have considered $Y_1v/\sqrt{2} \ll m_\chi < m_N$. Hence $m_{N_1} < m_{N_2}$. Therefore, N_1 becomes the stable DM candidate. From Equations (38, 39), one can write :

$$\begin{aligned}
 Y_1 &= -\frac{\Delta m \sin 2\theta}{\sqrt{2}v}, \\
 m_N &= m_{N_1} \sin^2\theta + m_{N_2} \cos^2\theta. \quad (41)
 \end{aligned}$$

where $\Delta m = m_{N_2} - m_{N_1}^2$ is the mass difference between the two mass eigenstates and m_N is the mass of electrically charged component of vector like fermion doublet N^- .

²We would like to remind the readers that N_1 and N_2 are not same as N_1^0 and N_2^0 . $N_{1,2}$ are the physical eigenstates arising out of the singlet (χ) doublet (N) admixture. Here, N_1 is the DM while N_2 is the NLSP. Where as, N_1^0 and N_2^0 are the two pseudo Dirac states that emerge from the neutral component (N^0) of the vector-like lepton doublet (N) due to the majorana mass term acquired by N^0 in presence of the scalar triplet Δ .

Therefore, one can express interaction terms of \mathcal{L}^{VF} in mass basis of N_1 and N_2 as

$$\begin{aligned} \mathcal{L}_{int}^{VF} = & \left(\frac{e_0}{2 \sin \theta_W \cos \theta_W} \right) \left[\sin^2 \theta \overline{N_1} \gamma^\mu Z_\mu N_1 + \cos^2 \theta \overline{N_2} \gamma^\mu Z_\mu N_2 \right. \\ & \left. + \sin \theta \cos \theta (\overline{N_1} \gamma^\mu Z_\mu N_2 + \overline{N_2} \gamma^\mu Z_\mu N_1) \right] \\ & + \frac{e_0}{\sqrt{2} \sin \theta_W} \sin \theta \overline{N_1} \gamma^\mu W_\mu^+ N^- + \frac{e_0}{\sqrt{2} \sin \theta_W} \cos \theta \overline{N_2} \gamma^\mu W_\mu^+ N^- \\ & + \frac{e_0}{\sqrt{2} \sin \theta_W} \sin \theta N^+ \gamma^\mu W_\mu^- N_1 + \frac{e_0}{\sqrt{2} \sin \theta_W} \cos \theta N^+ \gamma^\mu W_\mu^- N_2 \\ & - \left(\frac{e_0}{2 \sin \theta_W \cos \theta_W} \right) \cos 2\theta W N^+ \gamma^\mu Z_\mu N^- - e_0 N^+ \gamma^\mu A_\mu N^- \\ & - \frac{Y_1}{\sqrt{2}} h \left[\sin 2\theta (\overline{N_1} N_1 - \overline{N_2} N_2) + \cos 2\theta (\overline{N_1} N_2 + \overline{N_2} N_1) \right] \quad (42) \end{aligned}$$

The relevant DM phenomenology of the model then mainly depend on following three independent parameters :

$$\{ m_{N_1}, \Delta m, \sin \theta \} \quad (43)$$

5.1. Constraints on the Model Parameters

The model parameters are not totally free from theoretical and experimental bounds. Here we would like to discuss briefly the constraints coming from Perturbativity, invisible decay widths of Z and H , and corrections to electroweak parameters.

- **Perturbativity:** The upper limit of perturbativity bound on quartic and Yukawa couplings of the model are given by,

$$|Y_1| < \sqrt{4\pi}. \quad (44)$$

- **Invisible decay width of Higgs:** If the mass of DM is below $m_h/2$, then Higgs can decay to two invisible particles in final state and will yield invisible decay width. Recent Large Hadron Collider (LHC) data put strong constraint on the invisible branching fraction of Higgs to be $Br(h \rightarrow inv) \leq 0.24$ [80–82], which can be expressed as:

$$\frac{\Gamma(h \rightarrow inv.)}{\Gamma(h \rightarrow SM) + \Gamma(h \rightarrow inv.)} \leq 0.24, \quad (45)$$

where $\Gamma(h \rightarrow SM) = 4.2$ MeV for Higgs mass $m_h = 125.09$ GeV, obtained from recent measured LHC data [68]. Therefore, the invisible Higgs decay width is given by

$$\Gamma(h \rightarrow inv.) \leq 1.32 \text{ MeV}, \quad (46)$$

where

$$\begin{aligned} \Gamma(h \rightarrow inv.) = & \Gamma(h \rightarrow \overline{N_1} N_1). \quad (47) \\ = & \frac{1}{16\pi} (Y_1 \sin 2\theta)^2 m_h \left(1 - \frac{4m_{N_1}^2}{m_h^2} \right)^{\frac{3}{2}} \Theta(m_h - 2m_{N_1}), \end{aligned}$$

where the step function $\Theta(m_h - 2m_{N_1}) = 1$ if $m_{N_1} \leq m_h/2$ and is 0 if $m_{N_1} > m_h/2$. The decay width of Higgs to DM is proportional to $Y_1 = -\frac{\Delta m \sin 2\theta}{\sqrt{2}v}$. Therefore, it depends on the mass splitting with NLSP (Δm) as well as on the doublet singlet

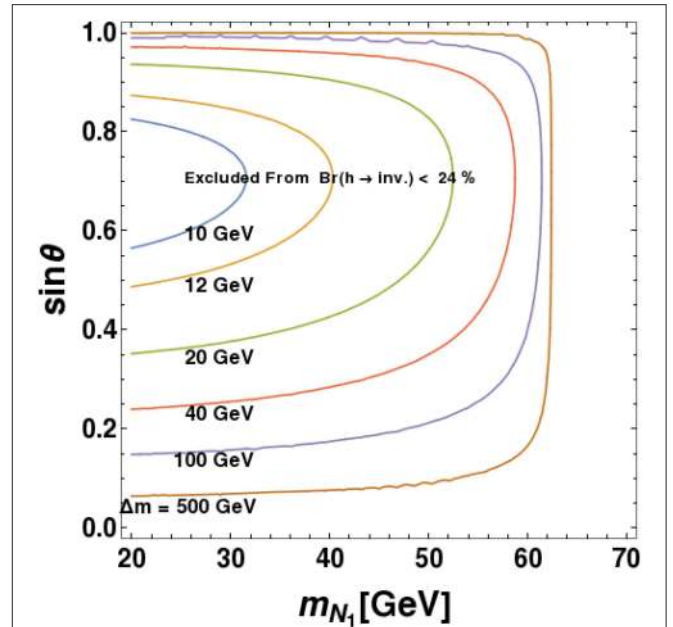


FIGURE 14 | Constraints from Higgs invisible decay width is shown in $m_{N_1} - \sin \theta$ plane. Here each contour line correspond to different value of Δm depicted in the figure. Inner region of each contour line excluded from Higgs invisible decay width, $\Gamma(h \rightarrow inv.) \leq 1.32$ MeV for a particular value of Δm .

mixing ($\sin \theta$). The invisible Higgs decay constraint on the model for $m_{N_1} < m_h/2$ is shown in **Figure 14**, where we have shown the exclusion in $M_{N_1} - \sin \theta$ plane for different choices of Δm ranging from 10 GeV to 500 GeV. The inner side of the contour is excluded. This essentially shows that with large $\Delta m \sim 500$ GeV, essentially all of $m_{N_1} \leq m_h/2$ is excluded, while for a small $\Delta m \sim 10$ GeV, the constraint is milder due to less Higgs decay width and excludes only regions for DM masses $M_{N_1} \leq 30$ GeV within $\sin \theta \sim \{0.6 - 0.8\}$. Therefore, even in $m_{N_1} \leq m_h/2$ region, if Δm and $\sin \theta$ are small, which turns out to be the case for satisfying relic density and direct search as we demonstrate later, then are allowed by the Higgs invisible decay constraint.

- **Invisible decay width of Z:** If the masses of dark sector particles are below $m_Z/2$, then Z can decay to dark sector particles leading to an increase of Z -decay width. However, from current observation, invisible decay width of Z boson is strongly bounded. The upper limit on invisible Z -decay width is given by Patrignani et al. [68]:

$$\Gamma(Z \rightarrow inv.) = 499.0 \pm 1.5 \text{ MeV}, \quad (48)$$

where the decay of Z to N_1 DM is given as:

$$\begin{aligned} \Gamma(Z \rightarrow \overline{N_1} N_1) = & \frac{1}{48\pi} \left(\frac{g \sin^2 \theta}{\cos \theta_W} \right)^2 m_Z \left(1 + \frac{2m_{N_1}^2}{m_Z^2} \right) \\ & \sqrt{1 - \frac{4m_{N_1}^2}{m_Z^2}} \Theta(m_Z - 2m_{N_1}). \quad (49) \end{aligned}$$

TABLE 3 | Global fit for the electroweak precision parameters taken from reference [87].

	$10^3\hat{S}$	$10^3\hat{T}$	10^3W	10^3Y
Light Higgs	0.0 ± 1.3	0.1 ± 0.9	0.1 ± 1.2	-0.4 ± 0.8

The Z -invisible decay does not play a crucial role in small $\sin\theta$ regions, which are required for the DM to achieve correct relic density, thus allowing almost all of the $M_{N_1} \leq m_Z/2$ parameter space of the model.

5.2. Corrections to the Electroweak Precision Parameters

Addition of a vector like fermion doublet to the SM gives correction to the electroweak precision test parameters S, T and U [83–86]. The values of these parameters are tightly constrained by experiments. The new observed parameters are in fact four in number \hat{S}, \hat{T}, W and Y [87], where the \hat{S}, \hat{T} are related to Peskin-Takeuchi parameters S, T as $\hat{S} = \alpha S/4 \sin^2\theta_w, \hat{T} = \alpha T$, while W and Y are two new set of parameters. The measured values of these parameters at LEP-I and LEP-II put a lower bound on the mass scale of vector like fermions. The result of a global fit of the parameters is presented in the **Table 3** for a light Higgs [87]³.

In the present scenario, we have a vector like doublet and a singlet fermion field are added to the SM. But the physical states are a charged fermion N^- , and two singlet doublet mixed neutral fermions N_1 (dominant singlet component) and N_2 (dominant doublet component). Therefore, the contribution to the precision parameters also depends on the mixing angle $\sin\theta$. The expression for \hat{S} in terms m_{N_1}, m_{N_2}, m_N and $\sin\theta$ of is given as Cynolter and Lendvai [88]:

$$\hat{S} = \frac{g^2}{16\pi^2} \left[\frac{1}{3} \left\{ \ln\left(\frac{\mu_{ew}^2}{m_{N_2}^2}\right) - \cos^4\theta \ln\left(\frac{\mu_{ew}^2}{m_{N_1}^2}\right) - \sin^4\theta \ln\left(\frac{\mu_{ew}^2}{m_{N_1}^2}\right) \right\} - 2 \sin^2\theta \cos^2\theta \left\{ \ln\left(\frac{\mu_{ew}^2}{m_{N_1}m_{N_2}}\right) + \frac{m_{N_1}^4 - 8m_{N_1}^2m_{N_2}^2 + m_{N_2}^4}{9(m_{N_1}^2 - m_{N_2}^2)^2} + \frac{(m_{N_1}^2 + m_{N_2}^2)(m_{N_1}^4 - 4m_{N_1}^2m_{N_2}^2 + m_{N_2}^4)}{6(m_{N_1}^2 - m_{N_2}^2)^3} \ln\left(\frac{m_{N_2}^2}{m_{N_1}^2}\right) + \frac{m_{N_1}m_{N_2}(m_{N_1}^2 + m_{N_2}^2)}{2(m_{N_1}^2 - m_{N_2}^2)^2} + \frac{m_{N_1}^3m_{N_2}^3}{(m_{N_1}^2 - m_{N_2}^2)^3} \ln\left(\frac{m_{N_2}^2}{m_{N_1}^2}\right) \right\} \right] \quad (50)$$

where μ_{ew} is at the EW scale.

In the left panel of **Figure 15**, we have plotted \hat{S} as a function of m_{N_2} keeping $m_{N_1} = 200$ GeV for different values of the mixing angle. In the right panel, we have shown the allowed values of

³The value \hat{S}, \hat{T}, W and Y are obtained using a Higgs mass $m_h = 115$ GeV. However, we now know that the SM Higgs mass is 125 GeV. Therefore, the value of \hat{S}, \hat{T}, W and Y are expected to change. But this effect is nullified by the small values of $\sin\theta$.

\hat{S} in the plane of $m_{N_2} - m_N$ vs. m_{N_2} for $\sin\theta = 0.05$ (Green Color), $\sin\theta = 0.1$ (Red color) and $\sin\theta = 0.2$ (Maroon color). We observed that \hat{S} does not put strong constraints on m_{N_1} and m_{N_2} . Moreover, small values of $\sin\theta$ allows a small mass splitting between N_2 and N^- which relaxes the constraint on \hat{T} parameter as we discuss below. The expression for \hat{T} is given as Cynolter and Lendvai [88]:

$$\hat{T} = \frac{g^2}{16\pi^2 M_W^2} \left[2 \sin^2\theta \cos^2\theta \Pi(m_{N_1}, m_{N_2}, 0) - 2 \cos^2\theta \Pi(m_N, m_{N_2}, 0) - 2 \sin^2\theta \Pi(m_N, m_{N_1}, 0) \right] \quad (51)$$

where $\Pi(a, b, 0)$ is given by:

$$\begin{aligned} \Pi(a, b, 0) = & -\frac{1}{2}(M_a^2 + M_b^2) \left(\text{Div} + \ln\left(\frac{\mu_{ew}^2}{M_a M_b}\right) \right) \\ & -\frac{1}{4}(M_a^2 + M_b^2) - \frac{(M_a^4 + M_b^4)}{4(M_a^2 - M_b^2)} \ln\frac{M_b^2}{M_a^2} \\ & + M_a M_b \left\{ \text{Div} + \ln\left(\frac{\mu_{ew}^2}{M_a M_b}\right) + 1 \right. \\ & \left. + \frac{(M_a^2 + M_b^2)}{2(M_a^2 - M_b^2)} \ln\frac{M_b^2}{M_a^2} \right\} \end{aligned} \quad (52)$$

with $\text{Div} = \frac{1}{\epsilon} + \ln 4\pi - \gamma_\epsilon$ contains the divergent term in dimensional regularization method. From the left panel of **Figure 16** we see that for $\sin\theta < 0.05$ we don't get strong constraints on m_{N_2} and m_{N_1} . Moreover, small values of $\sin\theta$ restricts the value of $m_{N_2} - m_N$ to be less than a GeV. As a result large m_{N_2} values are also allowed. Near $m_{N_2} \approx m_N, \hat{T}$ vanishes as expected. The value of Y and W are usually suppressed by the masses of new fermions. Since the allowed masses of N_1, N_2 and N^\pm are above 100 GeV by the relic density constraint (to be discussed later), so Y and W are naturally suppressed.

5.3. Relic Density of Singlet-Doublet Leptonic Dark Matter

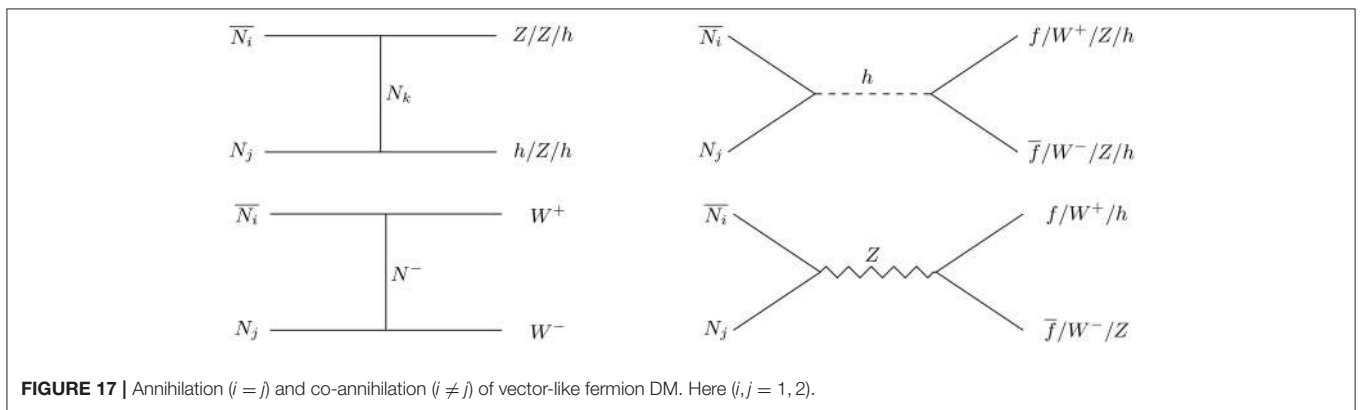
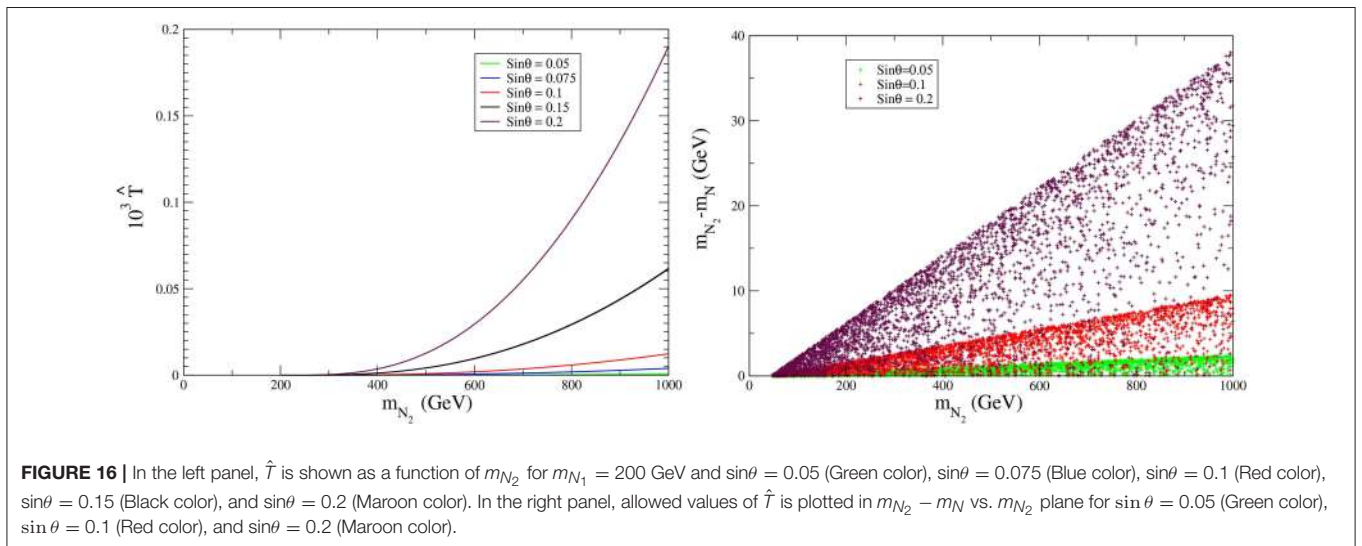
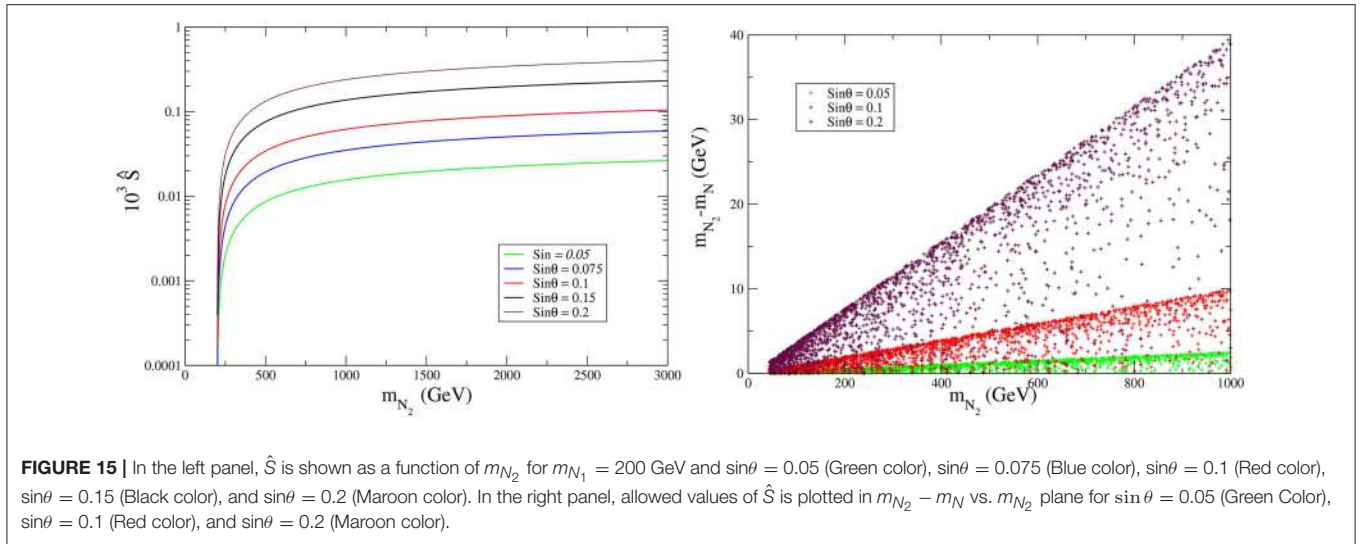
As stated earlier, the lightest stable physical state N_1 is the DM, which is an admixture of a singlet vector-like fermion (χ) and the neutral component of a vector-like fermionic doublet (N). Due to presence of mass hierarchy between dark sector particles N_1, N_2 and N^- , the lightest component N_1 not only annihilate with itself but also co-annihilate with N_2 and N^- to yield a net a relic density. The relevant diagrams are shown in **Figures 17–19**.

We assume all the heavier particles: N_2 and N^- in the dark sector ultimately decay to lightest stable particle N_1 . So in this scenario one can write the Boltzmann equation in terms of total number density $n = n_{N_1} + n_{N_2} + n_{N^\pm}$ as

$$\frac{dn}{dt} + 3Hn = -\langle\sigma v\rangle_{eff} (n^2 - n_{eq}^2), \quad (53)$$

where

$$\langle\sigma v\rangle_{eff} = \frac{g_1^2}{g_{eff}^2} \langle\sigma v\rangle_{N_1 N_1} + \frac{2g_1 g_2}{g_{eff}^2} \langle\sigma v\rangle_{N_1 N_2} \left(1 + \frac{\Delta m}{m_{N_1}}\right)^{\frac{3}{2}} e^{-x \frac{\Delta m}{m_{N_1}}}$$



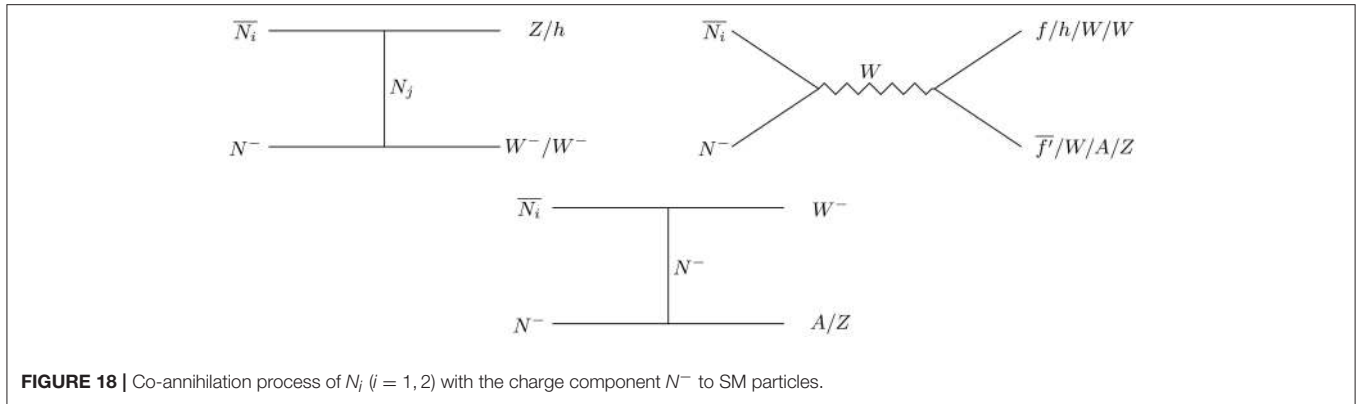


FIGURE 18 | Co-annihilation process of N_i ($i = 1, 2$) with the charge component N^- to SM particles.

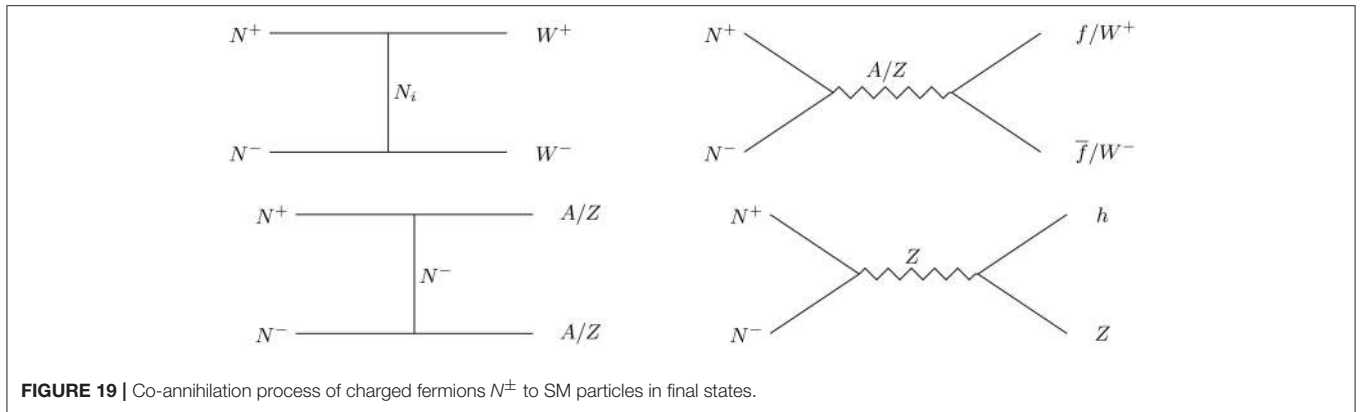


FIGURE 19 | Co-annihilation process of charged fermions N^\pm to SM particles in final states.

$$\begin{aligned}
 & + \frac{2g_1g_3}{g_{eff}^2} \langle \sigma v \rangle_{N_1 N^-} \left(1 + \frac{\Delta m}{m_{N_1}}\right)^{\frac{3}{2}} e^{-x \frac{\Delta m}{m_{N_1}}} \\
 & + \frac{2g_2g_3}{g_{eff}^2} \langle \sigma v \rangle_{N_2 N^-} \left(1 + \frac{\Delta m}{m_{N_1}}\right)^3 e^{-2x \frac{\Delta m}{m_{N_1}}} \\
 & + \frac{g_2^2}{g_{eff}^2} \langle \sigma v \rangle_{N_2 N_2} \left(1 + \frac{\Delta m}{m_{N_1}}\right)^3 e^{-2x \frac{\Delta m}{m_{N_1}}} \\
 & + \frac{g_3^2}{g_{eff}^2} \langle \sigma v \rangle_{N^+ N^-} \left(1 + \frac{\Delta m}{m_{N_1}}\right)^3 e^{-2x \frac{\Delta m}{m_{N_1}}}. \tag{54}
 \end{aligned}$$

In above equation, g_{eff} , defined as effective degrees of freedom, which is given by

$$g_{eff} = g_1 + g_2 \left(1 + \frac{\Delta m}{m_{N_1}}\right)^{\frac{3}{2}} e^{-x \frac{\Delta m}{m_{N_1}}} + g_3 \left(1 + \frac{\Delta m}{m_{N_1}}\right)^3 e^{-2x \frac{\Delta m}{m_{N_1}}}, \tag{55}$$

where g_1 , g_2 and g_3 are the degrees of freedom of N_1 , N_2 and N^- , respectively and $x = x_f = \frac{m_{N_1}}{T_f}$, where T_f is the freeze out temperature. Then the relic density of the N_1 DM can be given by Griest and Seckel [89], Chatterjee and Sahu [90], and Patra et al. [91]

$$\Omega_{N_1} h^2 = \frac{1.09 \times 10^9 \text{ GeV}^{-1}}{g_*^{1/2} M_{PL}} \frac{1}{J(x_f)}, \tag{56}$$

where $J(x_f)$ is given by

$$J(x_f) = \int_{x_f}^{\infty} \frac{\langle \sigma |v| \rangle_{eff}}{x^2} dx. \tag{57}$$

We note here that the freeze-out abundance of N_1 DM is controlled by the annihilation and co-annihilation channels as shown in **Figures 17–19**. Therefore, the important parameters which decide the relic abundance of N_1 are mass of DM (m_{N_1}), the mass splitting (Δm) between the DM and the next-to-lightest stable particle (NLSP) and the singlet-doublet mixing angle $\sin \theta$. Here we use MicrOmega [66] to calculate the relic density of N_1 DM.

Variation of relic density of N_1 DM is shown in **Figure 20** as a function of its mass, for a fixed $\Delta m = 10 - 100$ GeV (in left and right panels of **Figure 20**, respectively) and different choices of mixing angle $\sin \theta$. We note that the annihilation cross-section increases with $\sin \theta$, due to larger $SU(2)$ component, resulting in smaller relic density. The resonance drop at $m_Z/2$ and at $m_h/2$ is observed due to s -channel Z and H mediated contributions to relic abundance. Another important feature of **Figure 20** is that when Δm is small, relic density is smaller due to large co-annihilation contribution (less Boltzmann suppression followed from Equation 54). This feature can also be corroborated from **Figure 21**, where we have shown relic density as a function of DM mass by keeping a fixed range of $\sin \theta$ and chosen different possible Δm . Alternatively in **Figure 21**, we have shown relic

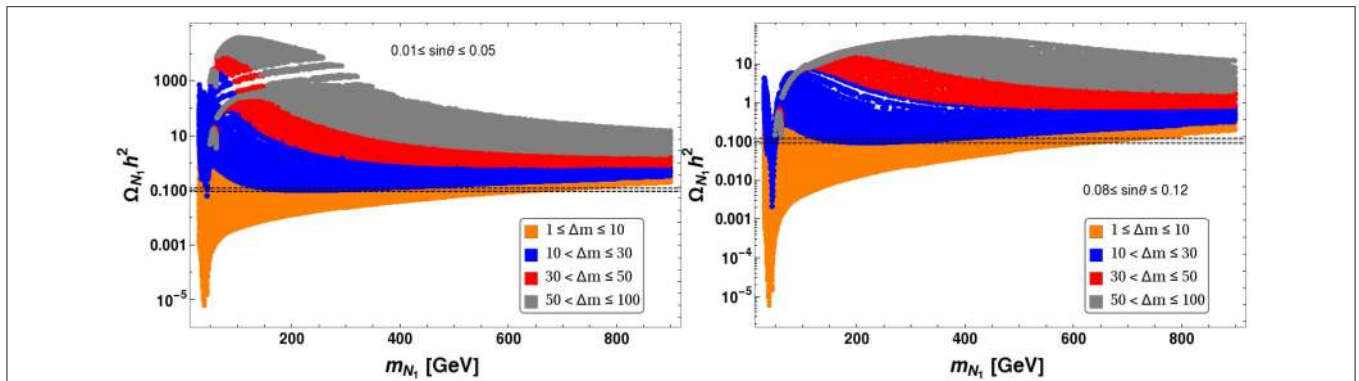


FIGURE 20 | Variation of relic density with DM mass m_{N_1} , keeping fixed range of $\sin \theta$: $0.01 \leq \sin \theta \leq 0.05$ (left panel) and $0.08 \leq \sin \theta \leq 0.12$ (right panel). The different color patches corresponds to different Δm region: $1 \leq \Delta m(\text{in GeV}) \leq 10$ (Orange), $10 < \Delta m(\text{in GeV}) \leq 30$ (Blue), $30 < \Delta m(\text{in GeV}) \leq 50$ (Red) and $50 < \Delta m(\text{in GeV}) \leq 100$ (Gray). Correct relic density, $0.1166 \leq \Omega h^2 \leq 0.1206$ is shown by black dashed line. All the masses are in GeVs.

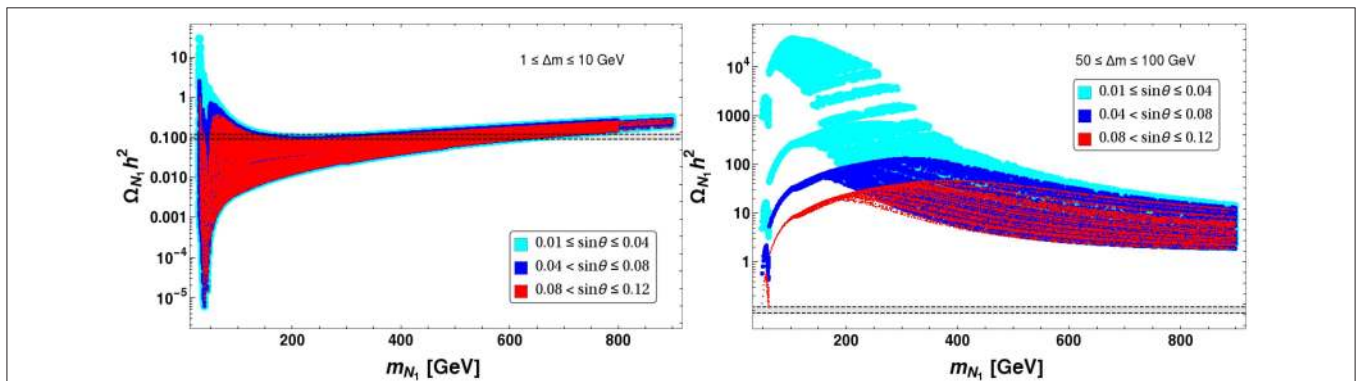


FIGURE 21 | Variation of relic density with DM mass m_{N_1} , keeping fixed region of Δm : $1 \leq \Delta m \leq 10$ GeV (left panel) and $50 \leq \Delta m \leq 100$ GeV (right panel). The different color patches are corresponding to different $\sin \theta$ region: $0.01 \leq \sin \theta \leq 0.04$ (Cyan), $0.04 < \sin \theta \leq 0.08$ (Blue), $0.08 < \sin \theta \leq 0.12$ (Red). Correct relic density, $0.1166 \leq \Omega h^2 \leq 0.1206$ is shown by black dashed line. All the masses are in GeVs.

density as a function of DM mass by keeping a fixed range of Δm , while varying $\sin \theta$. We see from the left panel of **Figure 21** that for small Δm co-annihilation dominates and hence the effect of $\sin \theta$ on relic abundance is quite negligible. On the other hand, from the right panel of **Figure 21**, we see that for large Δm , where co-annihilation is suppressed, the effect of $\sin \theta$ on relic abundance is clearly visible. For small $\sin \theta$, the effective annihilation cross-section is small which leads to large relic abundance, while for large $\sin \theta$ the relic abundance is small provided that the Δm is big enough to avoid co-annihilation contributions.

From **Figure 22**, we see that for a wide range of singlet-doublet mixing ($\sin \theta$), we can get correct relic abundance in the plane of m_{N_1} vs. Δm . Different ranges of $\sin \theta$ are indicated by different color codes. To understand our result, we divide the plane of m_{N_1} vs. Δm into two regions: (i) the bottom portion with small Δm , where Δm decreases with larger mass of N_1 , (ii) the top portion with larger mass splitting Δm , where Δm increases slowly with larger DM mass m_{N_1} . In the former case, for a given range of $\sin \theta$, the annihilation cross-section decreases for large mass of N_1 . Therefore, we need more co-annihilation contribution to compensate, which requires Δm to decrease. This also imply that the region below to each colored zone is under

abundant (small Δm implying large co-annihilation for a given mass of N_1), while the region above is over abundant (large Δm implying small co-annihilation for a given mass of N_1). To understand the allowed parameter space in region (ii), we first note that co-annihilation contribution is much smaller here due to large Δm , so the annihilation processes effectively contribute to relic density. Now, let us recall that the Yukawa coupling $Y \propto \Delta m \sin \theta$. Therefore, for a given $\sin \theta$, larger Δm can lead to larger Y and therefore larger annihilation cross-section to yield under abundance, which can only be tamed down to correct relic density by having a larger DM mass. Hence in case-(ii), the region above to each colored zone (allowed region of correct relic density) is under abundant, while the region below to each colored zone is over abundant. Thus, the over and under abundant regions of both cases (i) and (ii) are consistent with each other.

5.4. Constraints on Parameters From Direct Search of Singlet-Doublet Leptonic Dark Matter

Let us now turn to constraints on parameters from direct search of N_1 DM in terrestrial laboratories. Due to singlet-doublet mixing, the N_1 DM in direct search experiments can scatter

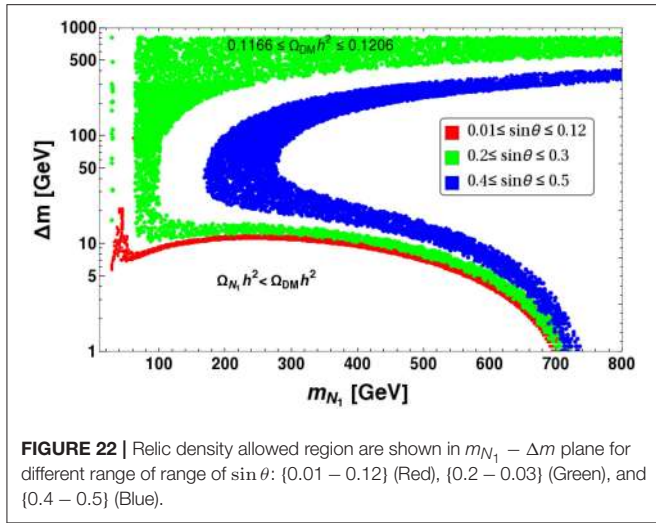


FIGURE 22 | Relic density allowed region are shown in $m_{N_1} - \Delta m$ plane for different range of range of $\sin \theta$: $\{0.01 - 0.12\}$ (Red), $\{0.2 - 0.03\}$ (Green), and $\{0.4 - 0.5\}$ (Blue).

off the target nucleus via Z and Higgs mediated processes as shown by the Feynman graphs in **Figure 23**. The cross-section per nucleon for Z-boson mediation is given by Goodman and Witten [92] and Essig [93]

$$\sigma_{SI}^Z = \frac{1}{\pi A^2} \mu_r^2 |\mathcal{M}|^2 \quad (58)$$

where A is the mass number of the target nucleus, $\mu_r = M_1 m_n / (M_1 + m_n) \approx m_n$ is the reduced mass, m_n is the mass of nucleon (proton or neutron) and \mathcal{M} is the amplitude for Z-boson mediated DM-nucleon cross-section given by

$$\mathcal{M} = \sqrt{2} G_F [\tilde{Z}(f_p/f_n) + (A - \tilde{Z})f_n \sin^2 \theta], \quad (59)$$

where f_p and f_n are the interaction strengths (including hadronic uncertainties) of DM with proton and neutron, respectively and \tilde{Z} is the atomic number of the target nucleus. On the other hand, the spin-independent DM-nucleon cross-section per nucleon mediated via the exchange of SM Higgs is given by:

$$\sigma_{SI}^h = \frac{1}{\pi A^2} \mu_r^2 [Z f_p + (A - Z) f_n]^2 \quad (60)$$

where the effective interaction strengths of DM with proton and neutron are given by:

$$f_{p,n} = \sum_{q=u,d,s} f_{Tq}^{(p,n)} \alpha_q \frac{m_{(p,n)}}{m_q} + \frac{2}{27} f_{TG}^{(p,n)} \sum_{q=c,t,b} \alpha_q \frac{m_{p,n}}{m_q} \quad (61)$$

with

$$\alpha_q = \frac{Y \sin 2\theta}{M_h^2} \left(\frac{m_q}{v} \right). \quad (62)$$

In Equation (61), the different coupling strengths between DM and light quarks are given by Bertone et al. [4] $f_{Tu}^{(p)} = 0.020 \pm 0.004$, $f_{Td}^{(p)} = 0.026 \pm 0.005$, $f_{Ts}^{(p)} = 0.118 \pm 0.062$, $f_{Tu}^{(n)} = 0.014 \pm$

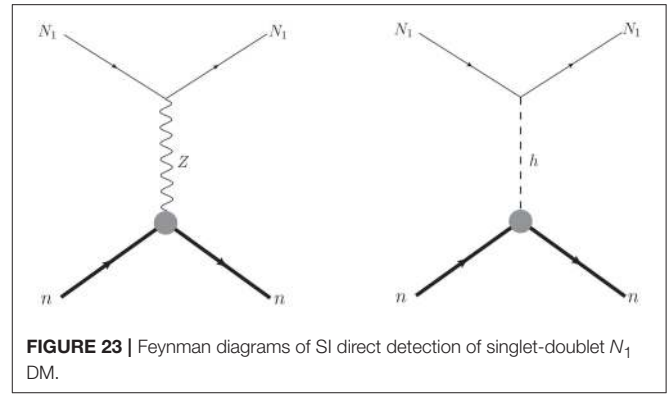


FIGURE 23 | Feynman diagrams of SI direct detection of singlet-doublet N_1 DM.

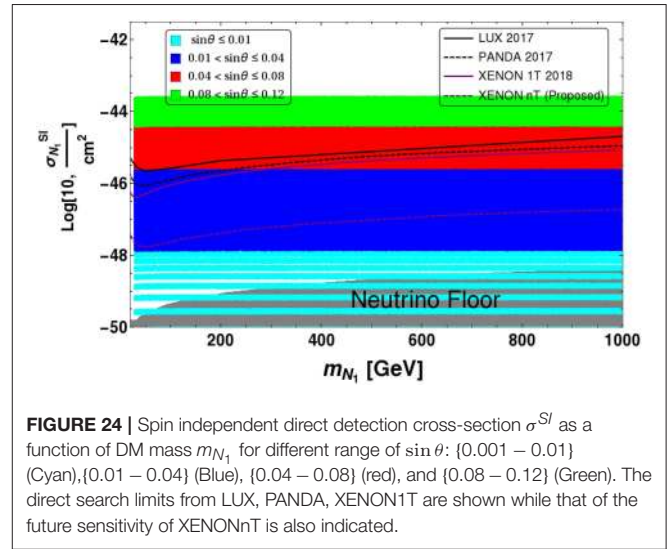


FIGURE 24 | Spin independent direct detection cross-section σ_{SI}^{SI} as a function of DM mass m_{N_1} for different range of $\sin \theta$: $\{0.001 - 0.01\}$ (Cyan), $\{0.01 - 0.04\}$ (Blue), $\{0.04 - 0.08\}$ (red), and $\{0.08 - 0.12\}$ (Green). The direct search limits from LUX, PANDA, XENON1T are shown while that of the future sensitivity of XENONnT is also indicated.

$0.004, f_{Td}^{(n)} = 0.036 \pm 0.008, f_{Ts}^{(n)} = 0.118 \pm 0.062$. The coupling of DM with the gluons in target nuclei is parameterized by

$$f_{TG}^{(p,n)} = 1 - \sum_{q=u,d,s} f_{Tq}^{(p,n)}. \quad (63)$$

Thus from Equations (60–63) the spin-independent DM-nucleon cross-section is given to be:

$$\sigma_{SI}^h = \frac{4}{\pi A^2} \mu_r^2 \frac{Y^2 \sin^2 2\theta}{M_h^4} \left[\frac{m_p}{v} \left(f_{Tu}^p + f_{Td}^p + f_{Ts}^p + \frac{2}{9} f_{TG}^p \right) + \frac{m_n}{v} \left(f_{Tu}^n + f_{Td}^n + f_{Ts}^n + \frac{2}{9} f_{TG}^n \right) \right]^2. \quad (64)$$

In the above equation the only unknown quantity is Y or $\sin 2\theta$ which can be constrained by requiring that σ_{SI}^h is less than the current DM-nucleon cross-sections.

Now we make a combined analysis by taking both Z and H mediated diagrams taken into account together. In **Figure 24**, we show the spin-independent cross-section for N_1 DM within its mass range $m_{N_1} : 1 - 1000$ GeV. The plot is obtained by varying $\sin \theta$ within $\{0.001 - 0.12\}$ with $\sin \theta = \{0.001 - 0.01\}$

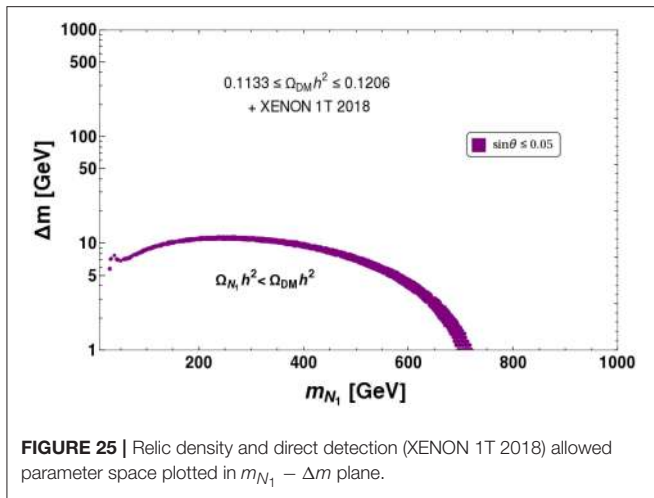


FIGURE 25 | Relic density and direct detection (XENON 1T 2018) allowed parameter space plotted in $m_{N_1} - \Delta m$ plane.

(Cyan), $\sin \theta = \{0.01 - 0.04\}$ (Blue), $\sin \theta = \{0.04 - 0.08\}$ (Red), $\sin \theta = \{0.08 - 0.12\}$ (Green). It clearly shows that the larger is $\sin \theta$, the stronger is the interaction strength (through larger contribution from Z mediation) and hence the larger is the DM-nucleon cross-section. Hence, it turns out that direct search experiments constraints $\sin \theta$ to a large extent. For example, we see that $\sin \theta \leq 0.04$, for the DM mass $m_{N_1} > 300$ GeV. The effect of Δm on DM-nucleon cross-section is less. However, we note that Δm plays a dominant role in the relic abundance of DM. Approximately, $\sin \theta \leq 0.05$ (Blue points) are allowed for most of the parameter space except for smaller DM masses. Cyan points indicate $\sin \theta < 0.01$. The discrete bands correspond to specific values of $\sin \theta$ chosen for the scan and essentially one can consider the whole region together to fall into this category which evidently have sensitivity close to neutrino floor. Note here, the scanned points in **Figure 24**, do not satisfy relic abundance.

Now let us turn to the parameter space, simultaneously allowed by observed relic density and latest constraints from direct DM search experiments, such as Xenon-1T. In **Figure 25**, we have shown the allowed parameter space again in $m_{N_1} - \Delta m$ plane. We see that null observation from direct search crucially tames down the relic density allowed parameter space to $\sin \theta < 0.05$ (Purple). **Figure 25** also shows that large singlet-doublet mixing, i.e., $\sin \theta \gtrsim 0.05$, allowed by correct relic density, is no more allowed by direct search limit in accordance with **Figure 24**.

We finally summarize the DM analysis of singlet doublet case here. The model offers an interesting phenomenology to exploit singlet-doublet mixing ($\sin \theta$) in accordance with DM mass (m_{N_1}) and the splitting with charged fermion content (Δm) to yield a large available parameter space for correct relic density. However, due to Z -mediated process contributing to direct detection of singlet-doublet leptonic dark matter, a stringent constraint on $\sin \theta \leq 0.05$ arises. This leads the DM to be allowed only in small Δm region (as in **Figure 25**) to achieve correct relic density through co-annihilation processes. However, this constraint can be relaxed in presence of a scalar triplet as we

discuss below. Moreover, the triplet can also give rise Majorana masses to light neutrinos (see section 4.2) through type-II seesaw to address DM and neutrinos in the same framework.

6. TRIPLET EXTENSION OF SINGLET-DOUBLET LEPTONIC DARK MATTER

6.1. Pseudo-Dirac Nature of Singlet-Doublet Leptonic Dark Matter

As discussed in section 5, the DM is assumed to be $N_1 = \cos \theta \chi + \sin \theta N^0$ with a Dirac mass m_{N_1} . However, from Equation (12) we see that the vev of Δ induces a Majorana mass to N_1 due to singlet-doublet mixing and is given by:

$$m_1 = \sqrt{2} f_N \sin^2 \theta \langle \Delta \rangle \approx f_N \sin^2 \theta \frac{-\mu v^2}{\sqrt{2} M_\Delta^2}. \quad (65)$$

Thus the N^0 has a large Dirac mass m_{N_1} and a small Majorana mass m as shown in the above Equation (65). Therefore, we get a mass matrix in the basis $\{N_{1L}, (N_{1R})^c\}$ as:

$$\mathcal{M} = \begin{pmatrix} m_1 & m_{N_1} \\ m_{N_1} & m_1 \end{pmatrix}. \quad (66)$$

Thus the Majorana mass m splits the Dirac spinor N_1 into two pseudo-Dirac states $\psi_{1,2}$ with mass eigenvalues $m_{N_1} \pm m$. The mass splitting between the two pseudo-Dirac states $\psi_{1,2}$ is given by

$$\delta m_1 = 2m_1 = 2\sqrt{2} f_N \sin^2 \theta \langle \Delta \rangle. \quad (67)$$

Note that $\delta m_1 \ll m_{N_1}$ from the estimate of induced vev of the triplet and hence does not play any role in the relic abundance calculation. However, the sub-GeV order mass splitting plays a crucial role in direct detection by forbidding the Z -boson mediated DM-nucleon elastic scattering. Now from Equations (20, 65) we see that the ratio:

$$R = \frac{M_v}{m_1} = \frac{f_L}{f_N \sin^2 \theta}. \quad (68)$$

Thus we see that for $R \sim 10^{-5}$ the ratio, $f_L/f_N \sim 10^{-3}$ if we assume $\sin \theta = 0.1$, which is much larger than the singlet-doublet mixing being used in section 5.4.

6.2. Effect of Scalar Triplet on Relic Abundance and Direct Search of Singlet-Doublet Dark Matter

We already have noted the diagrams that are present due to the addition of a scalar triplet for the ILD DM to freeze-out (see section 4.4). The main features of having an additional scalar triplet in the singlet-doublet DM model is very similar to what we have discussed before in case of ILD DM. The additional freedom that we have in case of singlet-doublet leptonic DM is to play with the mixing parameter $\sin \theta$ and Δm .

Let us first study relic density as a function of DM mass in presence of scalar triplet. This is shown in **Figure 26**, where we

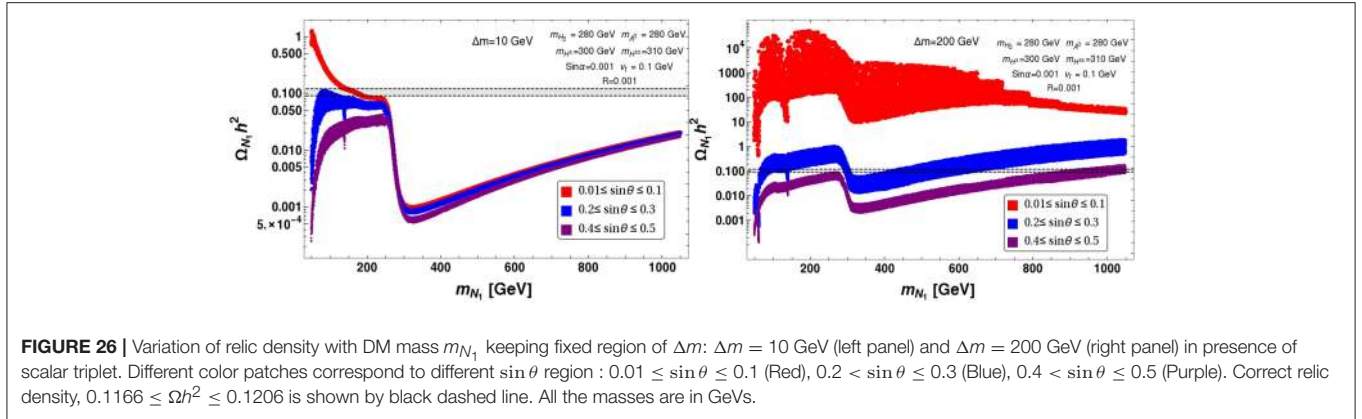


FIGURE 26 | Variation of relic density with DM mass m_{N_1} , keeping fixed region of Δm : $\Delta m = 10$ GeV (left panel) and $\Delta m = 200$ GeV (right panel) in presence of scalar triplet. Different color patches correspond to different $\sin \theta$ region : $0.01 \leq \sin \theta \leq 0.1$ (Red), $0.2 < \sin \theta \leq 0.3$ (Blue), $0.4 < \sin \theta \leq 0.5$ (Purple). Correct relic density, $0.1166 \leq \Omega h^2 \leq 0.1206$ is shown by black dashed line. All the masses are in GeVs.

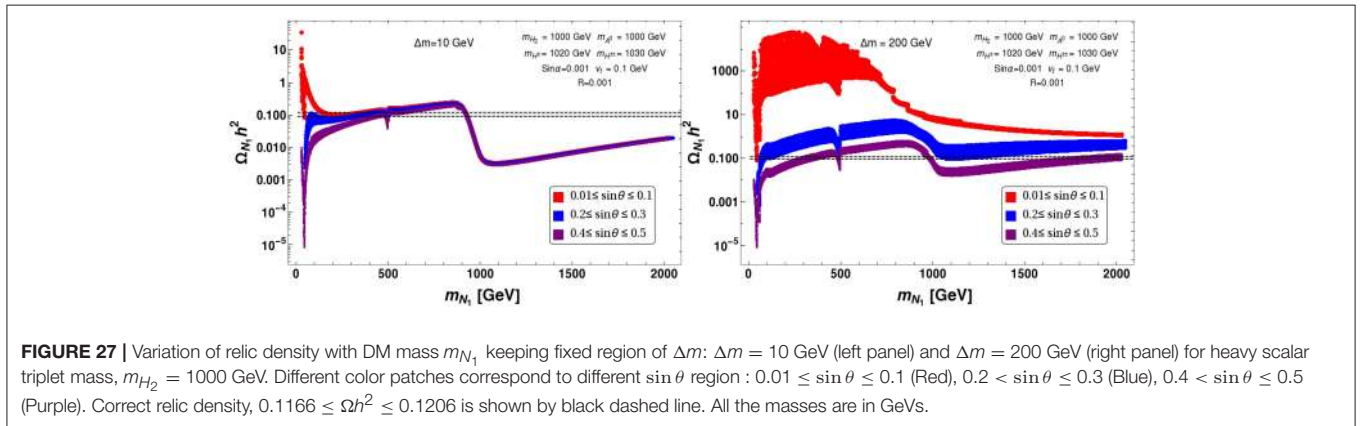


FIGURE 27 | Variation of relic density with DM mass m_{N_1} , keeping fixed region of Δm : $\Delta m = 10$ GeV (left panel) and $\Delta m = 200$ GeV (right panel) for heavy scalar triplet mass, $m_{H_2} = 1000$ GeV. Different color patches correspond to different $\sin \theta$ region : $0.01 \leq \sin \theta \leq 0.1$ (Red), $0.2 < \sin \theta \leq 0.3$ (Blue), $0.4 < \sin \theta \leq 0.5$ (Purple). Correct relic density, $0.1166 \leq \Omega h^2 \leq 0.1206$ is shown by black dashed line. All the masses are in GeVs.

choose two fixed values of $\Delta m = 10, 200$ GeV in left and right panel, respectively for a scalar triplet mass around 280 GeV. Different possible ranges of $\sin \theta$ are shown by different color codes. The main feature is again to see a drop in relic density near the value of the triplet mass, where the additional annihilation channel to the scalar triplet reduces relic density significantly. For small Δm , co-annihilation channels play an important part and therefore different mixing angles do not affect relic density significantly (compare left and right panel figures). Also due to large co-annihilation for small Δm as in the left panel, the relic density turns out to be much smaller than the right panel figure where Δm is large and do not offer the co-annihilation channels to be operative. An additional resonance drop at half of the triplet scalar mass is observed here (~ 140 GeV) due to s-channel triplet mediated processes.

A similar plot is shown in **Figure 27** with larger value of the scalar triplet mass ~ 1000 GeV. Obviously the features from **Figure 26**, is mostly retained where the drop in relic density is observed around ~ 1000 GeV and the drop is also smaller than what we had for smaller triplet mass.

Relic density allowed parameter space of the model in $m_{N_1} - \Delta m$ plane is shown in left panel of **Figure 28**. The bottom part of the allowed parameter space is again due to co-annihilation. For small $\sin \theta \sim 0.1$ (red points), this is the only allowed parameter space except the resonance at the extreme left hand side. For

larger $\sin \theta$, the resonance drops of doublet and triplet scalars also yield correct relic density. There is an under-abundant region when the triplet channel opens up, which is then reduced with larger DM mass. Therefore, it ends up with two different patches (both for blue and purple points) to be allowed below and above the scalar triplet mass. The direct search constraint in presence of scalar triplet thankfully omits the Z mediated diagram due to the pseudo-Dirac splitting and allows a larger $\sin \theta \sim 0.3$. However, in addition to the Yukawa coupling (Y) initiated SM Higgs mediation, there is an added contribution from the heavy Higgs due to the doublet triplet mixing. We have already seen before that the effect of the additional contribution to direct search cross-section is small in the small $\sin \alpha$ limit with a moderate choice of f_N . Therefore, we have omitted such contributions in generating the direct search allowed parameter space of the model as shown in the right panel of **Figure 28**. This again depicts that the model in presence of scalar triplet earns more freedom in relaxing Δm and $\sin \theta$ to some extent.

7. COLLIDER SIGNATURES

Finally, we discuss the collider signature of the model, which can be subdivided into two categories: (i) Displaced vertex signature and (ii) Excess in leptonic final states.

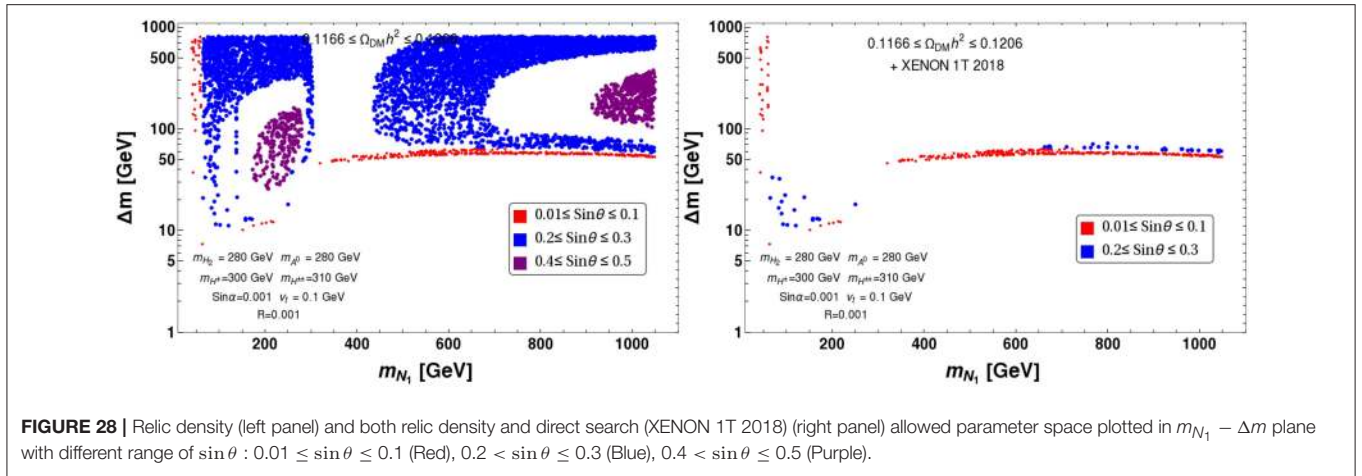


FIGURE 28 | Relic density (left panel) and both relic density and direct search (XENON 1T 2018) (right panel) allowed parameter space plotted in $m_{N_1} - \Delta m$ plane with different range of $\sin \theta$: $0.01 \leq \sin \theta \leq 0.1$ (Red), $0.2 < \sin \theta \leq 0.3$ (Blue), $0.4 < \sin \theta \leq 0.5$ (Purple).

7.1. Displaced Vertex Signature

In the small $\sin \theta$ limit, the charged inert fermion can show a displaced vertex signature. If the mass difference between the N^- and N_1 is greater than W^- mass then N^- can decay via a two body process. But if the mass difference is smaller than M_W , then N^- can decay via three body process say $N^- \rightarrow N_1 l^- \bar{\nu}_l$. The three body decay width is given as Bhattacharya et al. [53]:

$$\Gamma = \frac{G_F^2 \sin^2 \theta}{24\pi^3} m_N^5 I \tag{69}$$

where G_F is the Fermi coupling constant and I is given as:

$$I = \frac{1}{4} \lambda^{1/2} (1, a^2, b^2) F_1(a, b) + 6F_2(a, b) \ln \left(\frac{2a}{1 + a^2 - b^2 - \lambda^{1/2}(1, a^2, b^2)} \right) \tag{70}$$

In the above Equation $F_1(a, b)$ and $F_2(a, b)$ are two polynomials of $a = m_{N_1}/m_N$ and $b = m_l/m_N$, where m_l is the charged lepton mass. Up to $\mathcal{O}(b^2)$, these two polynomials are given by

$$\begin{aligned} F_1(a, b) &= (a^6 - 2a^5 - 7a^4(1 + b^2) + 10a^3(b^2 - 2) \\ &\quad + a^2(12b^2 - 7) + (3b^2 - 1)) \\ F_2(a, b) &= (a^5 + a^4 + a^3(1 - 2b^2)) \end{aligned} \tag{71}$$

In Equation (70), $\lambda^{1/2} = \sqrt{1 + a^4 + b^4 - 2a^2 - 2b^2 - 2a^2b^2}$ defines the phase space. In the limit $b = m_l/m_N \rightarrow 1 - a = \delta M/m_N$, $\lambda^{1/2}$ goes to zero and hence $I \rightarrow 0$. The life time of N^- is then given by $\tau \equiv \Gamma^{-1}$. We take the freeze out temperature of DM to be $T_f = m_{N_1}/20$. Since the DM freezes out during radiation dominated era, the corresponding time of DM freeze-out is given by:

$$t_f = 0.301 g_\star^{-1/2} \frac{m_{Pl}}{T_f^2}, \tag{72}$$

where g_\star is the effective massless degrees of freedom at a temperature T_f and m_{Pl} is the Planck mass. Demanding that N^- should decay before the DM freezes out (i.e., $\tau \lesssim t_f$) we get

$$\begin{aligned} \sin \theta &\gtrsim 1.1789 \times 10^{-5} \left(\frac{1.375 \times 10^{-5}}{I} \right)^{1/2} \left(\frac{200 \text{ GeV}}{m_N} \right)^{5/2} \\ &\left(\frac{g_\star}{106.75} \right)^{1/4} \left(\frac{m_{N_1}}{180 \text{ GeV}} \right). \end{aligned} \tag{73}$$

The lower bound on the mixing angle depends on the mass of N^- and N_1 . For a typical value of $m_N = 200$ GeV, $m_{N_1} = 180$ GeV, we get $\sin \theta \gtrsim 1.17 \times 10^{-5}$. Since τ is inversely proportional to m_N^5 , larger the mass, smaller will be the lower bound on the mixing angle.

To explore more whether we can get the relic abundance and displaced vertex simultaneously, we have shown in **Figure 29** relic abundance as a function of DM mass keeping the mass splitting $\Delta M \leq 50$ GeV and $\sin \theta = 10^{-4}$. In this small mixing angle limit there are coannihilation channels (see **Figure 19**) which are independent of $\sin \theta$ contributes to relic density. We choose the set of points which are giving us the correct relic density and tried to find the displaced vertex value. We have plotted in the right panel of **Figure 29** displaced vertex (Γ^{-1}) as a function of m_N . We can see that in the large mass of m_N , the displaced vertex is very small as expected as Γ^{-1} decreases with increase in mass. For larger mixing angles displaced vertex is suppressed. Again $\sin \theta$ cannot be arbitrarily small as shown in Equation (73), so Γ^{-1} will not be very large.

7.2. Hadronically Quiet Dilepton Signature

Since our proposed scenario have one vector like leptonic doublet, there is a possibility of producing charge partner pair of the doublet ($N^+ N^-$) at proton collider (LHC). The decay of N^\pm further produce leptonic final states through on-shell/off-shell W^\pm mediator to yield opposite sign dilepton plus missing energy as is shown in **Figure 30**. Obviously, W can decay to jets as well, to yield single lepton plus two jets and missing energy signature or that of four jets plus missing energy signature. But, LHC being a QCD machine, the jet rich final states are prone to

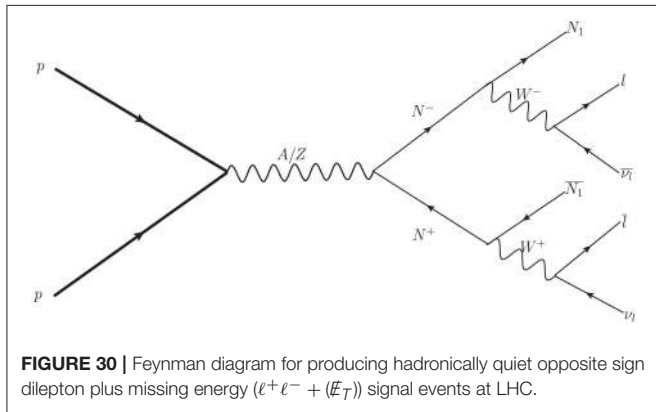
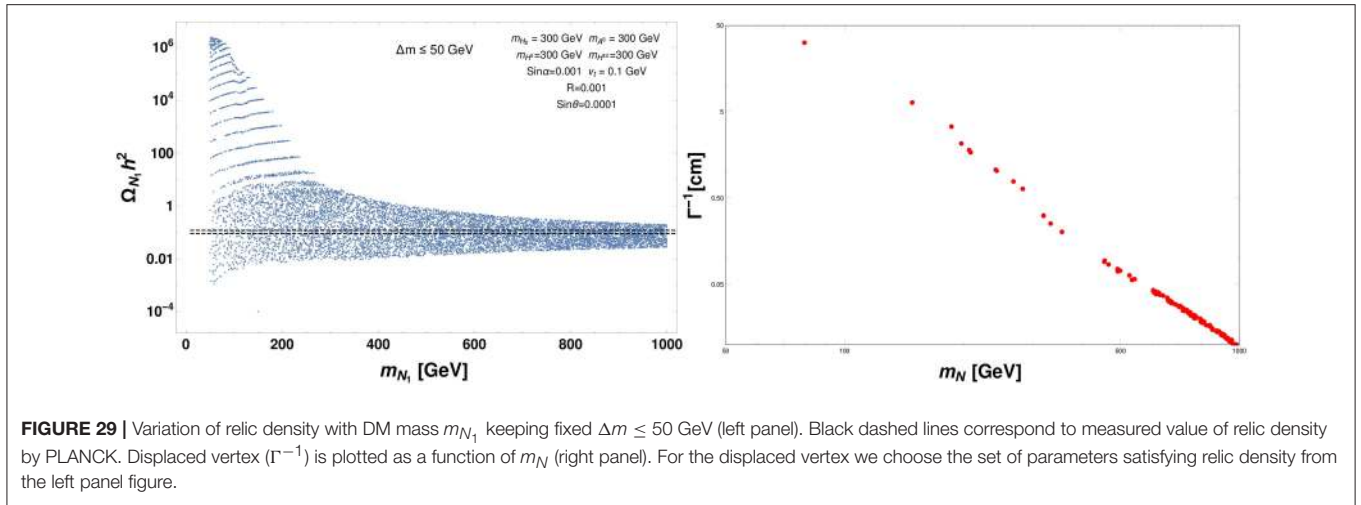


TABLE 4 | DM mass, $\sin \theta$, $\Delta m = m_{N^\pm} - m_{N^0}$, relic density, and SI direct search cross-sections of two benchmark points are mentioned for collider study.

BPs	$\{m_{N_1}, \sin \theta\}$	Δm	$\Omega_{N_1} h^2$	$\sigma_{N_1}^{SI}$ (in cm^2)	DM models
BP1	{ 141, 0.03 }	10	0.1201	7.6×10^{-47}	Doublet singlet DM
BP2	{ 50, 0.102 }	147	0.1165	1.2×10^{-47}	Doublet singlet DM + Triplet scalar

BP1 correspond to singlet doublet fermion DM scenario. BP2 depicts the case of singlet doublet DM model with an additional triplet in the picture. Note here that others parameters for BP2 remains same mentioned inset of the **Figure 28**.

very heavy SM background and cannot be segregated from that of the signal. We therefore refrain from calculating the other two possibilities here. A detailed analysis of collider signature of this model will be addressed in Barman et al. [94].

Doublet-singlet fermion DM in absence or in presence of scalar triplet do not distinguish to yield a different final state from that of $\ell^+ \ell^- + (\cancel{E}_T)$ shown in **Figure 30**. However, there is an important distinction that we discuss briefly here. $N^+ N^-$ production cross-section depends on the charge lepton masses and nothing else, leptonic decay branching fraction is also fixed. However, the splitting between DM (N^0) and its charged partner (N^\pm) ($\Delta m = m_{N^\pm} - m_{N^0}$) is seen in the missing energy distribution. The signal can only be segregated from that of the SM background when the splitting is large and it falls within the heaps of SM background when Δm is small. This feature can distinguish between the two cases of singlet doublet DM in presence and in absence of scalar triplet. To illustrate, we choose two benchmark points from two scenarios: *i*) doublet singlet leptonic DM (BP1) in absence of scalar triplet and *ii*) doublet singlet leptonic DM in presence of triplet (BP2), shown in **Table 4**. For BP1, we see that $\Delta m = 10$ GeV, has to be very small because relic density and direct search (XENON 1T 2018) put strong constraint on $\Delta m (\leq 12$ GeV). On the other hand, presence of triplet in this scenario can relax the situation to some

extent, and one may choose large $\Delta m \sim 150$ GeV for low DM mass (~ 50 GeV) and obey both relic density and direct search constraint, as indicated in BP2. Again, we note here, that such a low DM mass is still allowed by the Invisible Higgs data due to small $\sin \theta$ that we have taken here.

To study the collider signature of the model, we first implemented the model in **FeynRule** [95]. To generate events files, we used **Madgraph** [96] and further passed to **Pythia** [97] for analysis. We have imposed further selection cuts on leptons ($\ell = e, \mu$) and jets as follows to mimic the actual collider environment:

- **Lepton isolation:** Leptons are the main constituent of the signal. We impose transverse momentum cut of $p_T > 20$ GeV, pseudorapidity of $|\eta| < 2.5$ and separation cut $\Delta R \geq 0.2$ for separating from other leptons. Additionally, $\Delta R \geq 0.4$ is required to separate the leptons from jets. The definition of separation in azimuthal-pseudorapidity plane is $\Delta R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2}$.
- **Jet formation and identification** is performed in Pythia. We use cone-algorithm and impose that the jet initiator parton must have $p_T \geq 20$ GeV and forms a jet within a cone of $\Delta R \leq 0.4$. Jets are required to be defined for our events as to have zero jets.

Using above basic cuts, we have studied hadronically quite opposite signed dilepton final states :

$$\text{Signal} :: \ell^+ \ell^- + (\cancel{E}_T): \quad p p \rightarrow N^+ N^-, (N^- \rightarrow \ell^- \bar{\nu}_\ell N_1),$$

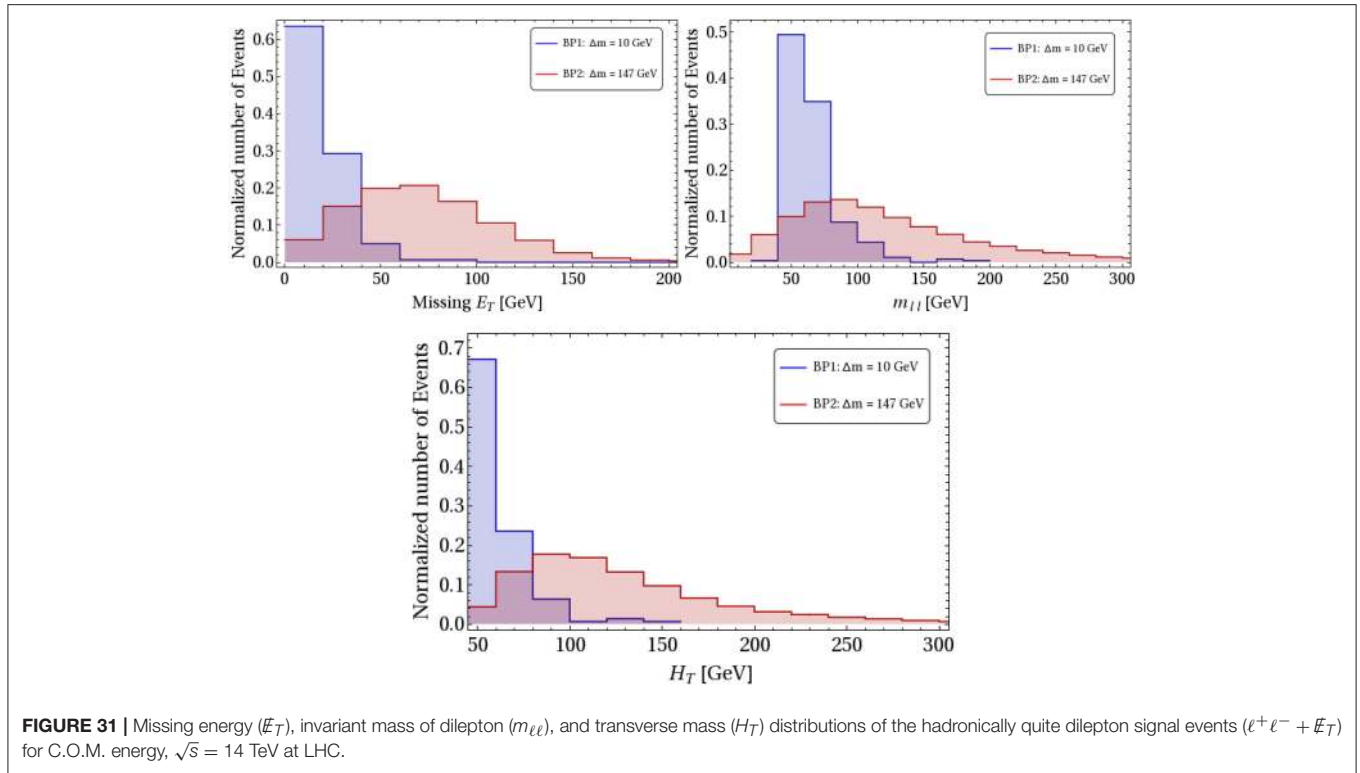


FIGURE 31 | Missing energy (E_T), invariant mass of dilepton ($m_{\ell\ell}$), and transverse mass (H_T) distributions of the hadronically quiet dilepton signal events ($\ell^+\ell^- + \cancel{E}_T$) for C.O.M. energy, $\sqrt{s} = 14$ TeV at LHC.

$$(N^+ \rightarrow \ell^+ \nu_\ell \bar{N}_1), \text{ where } \ell = e, \mu .$$

The distribution of signal events with respect to missing Energy (E_T), invariant mass of OSD ($m_{\ell\ell}$) and effective momentum (H_T) is shown in **Figure 31**, respectively top left, top right and bottom panel. We see that each of the distribution becomes flatter and the peak is shifted to higher energy value with larger Δm . As we have already mentioned that SM background yields a very similar distribution to that of BP1 and therefore cannot be segregated from small Δm cases. For details of background estimate and distribution, see for example, [98]. Without further selection cuts, the signals constitute a very tiny fraction of hadronically quiet dilepton channel at LHC. To reduce SM background, further selection cuts must be employed:

- $m_{\ell\ell} < |m_z - 15|$ and $m_{\ell\ell} > |m_z + 15|$,
- $H_T > 100, 200$ GeV,
- $E_T > 100, 200$ GeV.

We see that the signal events for BP1, after such a cut is reduced significantly, while for BP2, we are still left with moderately large number of events as shown in **Table 5**.

To summarize, we point out that singlet-doublet fermion DM can possibly yield a displaced vertex signature out of the charged fermion decay, thanks to small mass splitting and small $\sin \theta$, while due to the same reason, seeing an excess in leptonic final state will be difficult. On the other hand, the model where singlet-doublet fermion DM is extended with a scalar triplet satisfy relic density and direct search with a larger mass splitting between the DM and charged companion which allows such a case to yield a lepton excess to be probed at LHC, but the

TABLE 5 | Signal events for above mentioned benchmark points with $\sqrt{s} = 14$ TeV at the LHC for the luminosity $\mathcal{L} = 100 \text{ fb}^{-1}$ after E_T, H_T and $m_{\ell\ell}$ cuts.

BPs	Δm (GeV)	$\sigma_{pp \rightarrow N^+ N^-}$ (fb)	E_T (GeV)	H_T (GeV)	σ^{OSD} (fb)	$N_{\text{eff}}^{\text{OSD}} = \sigma^{\text{OSD}} \times \mathcal{L}$
BP1	10	12.01	>100	>100	< 0.0003	< 1
			>100	>100	0.711	71
BP2	147	33.11	>200	>200	0.250	25
			>100	>200	0.040	4
			>200	>200	0.039	4

displaced vertex signature may get subdued due to this. The complementarity of the two cases will be elaborated in Barman et al. [94]. We also note that scalar triplet extension do not allow the fermion DM to have any mass to also accommodate large Δm . This is only possible in the vicinity of Higgs resonance. We can however, earn a freedom on choosing a large Δm at any fermion mass value in the presence of a second DM component and see a lepton signal excess as has been pointed out in Barman et al. [94].

8. CONCLUSIONS AND FUTURE DIRECTIONS

Vector like leptons stabilized by a symmetry, provide a simple solution to DM problem of the universe. The relic density allowed parameter space provide a wide class of phenomenological implications to be explored in DM direct search experiments and in collider searches through signal excess or displaced vertex. In this article, we have provided a thorough analysis of different possible models in such a category. The results have been illustrated with parameter space scans, taking into account

the constraints coming from non-observation of DM in present direct search data, constraints from electroweak precision tests, vacuum stability, invisible decay widths of Higgs and Z etc., to see the allowed region where the model(s) can be probed in upcoming experiments.

We first reviewed the possibility of vector-like leptonic singlet χ , doublet N and their combination $\chi - N$ as viable candidates of DM. First we discussed about a vector-like singlet leptonic DM χ . In this case, the DM can only couple to visible sector through non-renormalizable dimension-5 operator $\bar{\chi}\chi H^\dagger H/\Lambda$, where Λ denotes a new physics (NP) scale. We find relic density allowed parameter space of the model requires Λ to be 500 GeV or less for DM mass ranging between 100 GeV to 500 GeV. However, the direct search cross-section for such Λ is much larger than the constraints obtained from XENON1T data. Therefore, a singlet lepton is almost ruled out being a viable candidate of DM.

We then discussed the possibility of neutral component of a vector-like inert lepton doublet (ILD) N^0 to be a viable DM candidate. Since the doublet has only gauge interaction, the correct relic abundance can be obtained only at heavy DM mass around \sim TeV. Again, the doublet DM suffers a stringent constraint from Z -mediated elastic scattering at direct search experiments. The relic density allowed parameter space therefore lies way above than the XENON1T bound of not observing a DM in direct search experiment. Therefore, an ILD DM alone is already ruled out. However, we showed that in presence of a scalar triplet, an ILD DM can be reinstated by forbidding the Z -mediated elastic scattering with the nucleons thanks to pseudo Dirac splitting. Due to additional interaction of ILD in presence of a scalar triplet, the mass of ILD DM is pushed to a higher side to achieve correct relic density. Moreover, the scalar triplet mixes with the SM doublet Higgs and paves a path for detecting the ILD DM at terrestrial laboratories. The presence of scalar triplet also yield a non-zero neutrino mass to three flavors of active neutrinos which are required by oscillation data. However, we noticed that the parameter space of an ILD DM is very limited to a very high mass due to its gauge coupling.

We then searched for a combination of singlet χ and neutral component of doublet $N = (N^-, N^0)$ being a viable candidate of DM. This is possible if both of the fermion fields possess same Z_2 symmetry. They mix after electroweak symmetry breaking. In fact, we found that the appropriate combination of a

singlet-doublet can be a viable DM candidate in a large parameter space spanning DM mass between Z resonance to \sim 700 GeV. The singlet-doublet mixing plays a key role in deciding the relic abundance of DM as well as detecting it in terrestrial laboratories. In fact, we found that a large singlet component admixture with a small doublet component is an appropriate combination to be a viable candidate for DM, particularly to meet direct search bounds ($\sin\theta \leq 0.05$). However, it is difficult for a DM with large singlet component to yield correct relic density due to small annihilation cross-section. Therefore, it has to depend heavily on co-annihilation to make up the small annihilation cross section, which in turn requires a small mass difference between the DM N_1 and its partners N^\pm, N_2 . In particular, if the mixing angle is very small (around $\sin\theta \sim 10^{-4}$), the decay of NLSP ($N^- \rightarrow N_1 + l^- + \bar{\nu}_l$) gives a measurable displaced vertex signature at LHC, aided by a small mass difference of N^- with the DM (N_1). However, this typical feature makes it difficult to identify any signal excess from production of the NLSP at LHC.

The situation becomes more interesting in presence of a scalar triplet. The latter, not only enhances the allowed parameter space of singlet-doublet mixed DM (by allowing a larger mixing $\sin\theta \lesssim 0.2$ and also a larger mass splitting between NLSP and DM), but also generates masses to three flavors active neutrinos via type-II seesaw. Presence of scalar triplet may also pave the path to discover this model through hadronically quiet dilepton channel at LHC. We would also like to add here that if the DM (singlet-doublet admixture) including the SM particles are charged under an additional flavor symmetry, say A_4 , then non-zero value of θ_{13} can be obtained from the flavor charge of DM, which has been elaborated in Bhattacharya et al. [99, 100].

AUTHOR CONTRIBUTIONS

All authors listed have made a substantial, direct and intellectual contribution to the work, and approved it for publication.

ACKNOWLEDGMENTS

We thank Basabendu Barman for helpful discussions. SB would like to acknowledge the support from DST-INSPIRE faculty grant IFA-13-PH-57 at IIT Guwahati. PG also like to thank MHRD, Government of India for research fellowship.

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Conflict of Interest Statement: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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APPENDIX A: COUPLINGS OF ILD DARK MATTER WITH SCALAR TRIPLETS AND SM PARTICLES

Trilinear vertices involving ILD and triplet Scalar:

$$\begin{aligned}
 \overline{(N^-)^c} N^- H^{++} &: & \sqrt{2} f_N \\
 \overline{(N^-)^c} N^0 H^+ &: & f_N \\
 \overline{(N^0)^c} N^0 H_1 &: & -\sin \alpha f_N \\
 \overline{(N^0)^c} N^0 H_2 &: & -\cos \alpha f_N \\
 \overline{(N^0)^c} N^0 A^0 &: & -i f_N
 \end{aligned} \tag{A1}$$

Trilinear vertices involving triplet scalars:

$$\begin{aligned}
 H^{++} H^- H^- &: & \sqrt{2} v_t \lambda_3 & \propto & 1/v_t \\
 H^{++} H^- H_2 &: & -\left(2 \cos \alpha v_t \lambda_2 - \sin \alpha v_t \lambda_1\right) \\
 & \xrightarrow{\sin \alpha \rightarrow 0} & -2 v_t \lambda_2 & \propto & 1/v_t \\
 H^{++} H^- H_1 &: & -\left(\cos \alpha v_t \lambda_1 + 2 \sin \alpha v_t \lambda_2\right)
 \end{aligned} \tag{A2}$$

Trilinear vertices involving ILD and SM particles:

$$\begin{aligned}
 \overline{N^0} N^- W^+ &: & \frac{e_0}{\sqrt{2} \sin \theta_W} \gamma^\mu \\
 N^- N^+ Z &: & -\frac{e_0}{\sin 2\theta_W} \cos 2\theta_W \gamma^\mu \\
 N^- N^+ A &: & -e_0 \gamma^\mu \\
 \overline{N^0} N^0 Z &: & \frac{e_0}{\sin 2\theta_W} \gamma^\mu
 \end{aligned} \tag{A3}$$